

# Mass Rules, Shell Models and the Structure of Hadrons

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FIAS Kolloquium

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# origin of the idea

1971 p-p elastic at ISR: kink in  $d\sigma/dt$

1972 no quarks found at the ISR

1973 e-p DIS at SLAC:

point-like spin  $\frac{1}{2}$  partons, gluons, sea, ..

what are the partons, if not the quarks?

**idea**, looking at decays in PDG listings:

## the stable leptons

count number of stable leptons in decays,  
(gamma = 2): muon = 3, pion = 4, ...

-> N(leptons) proportional to the mass;

shell structure like in atoms and nuclei?

-> identify 4 shells: pi, K, p,  $\Omega$

## A SCHEMATIC MODEL OF BARYONS AND MESONS \*

M. GELL-MANN

*California Institute of Technology, Pasadena, California*

Received 4 January 1964

If we assume that the strong interactions of baryons and mesons are correctly described in terms of the broken "eightfold way" <sup>1-3</sup>, we are tempted to look for some fundamental explanation of the situation. A highly promised approach is the purely dynamical "bootstrap" model for all the strongly interacting particles within which one may try to derive isotopic spin and strangeness conservation and broken eightfold symmetry from self-consistency alone <sup>4</sup>). Of course, with only strong interactions, the orientation of the asymmetry in the unitary space cannot be specified; one hopes that in some way the selection of specific components of the F-spin by electromagnetism and the weak interactions determines the choice of isotopic spin and hypercharge directions.

Even if we consider the scattering amplitudes of strongly interacting particles on the mass shell only and treat the matrix elements of the weak, electromagnetic, and gravitational interactions by means

ber  $n_t - n_{\bar{t}}$  would be zero for all known baryons and mesons. The most interesting example of such a model is one in which the triplet has spin  $\frac{1}{2}$  and  $z = -1$ , so that the four particles  $d^-$ ,  $s^-$ ,  $u^0$  and  $b^0$  exhibit a parallel with the leptons.

A simpler and more elegant scheme can be constructed if we allow non-integral values for the charges. We can dispense entirely with the basic baryon  $b$  if we assign to the triplet  $t$  the following properties: spin  $\frac{1}{2}$ ,  $z = -\frac{1}{3}$ , and baryon number  $\frac{1}{3}$ . We then refer to the members  $u^{\frac{2}{3}}$ ,  $d^{-\frac{1}{3}}$ , and  $s^{-\frac{1}{3}}$  of the triplet as "quarks" <sup>6</sup>)  $q$  and the members of the anti-triplet as anti-quarks  $\bar{q}$ . Baryons can now be constructed from quarks by using the combinations  $(qqq)$ ,  $(qqq\bar{q})$ , etc., while mesons are made out of  $(q\bar{q})$ ,  $(qq\bar{q}\bar{q})$ , etc. It is assuming that the lowest baryon configuration  $(qqq)$  gives just the representations 1, 8, and 10 that have been observed, while the lowest meson configuration  $(q\bar{q})$  similarly gives just 1 and 8.

P. Palazzi

1975 (unpublished)

## Indicazioni di una struttura a shell delle particelle e conseguenze relative

Elaborato presentato al concorso-esame per l' "Idoneità" al  
grado di RS (ricercatore) dell' INFN.

giugno 1975

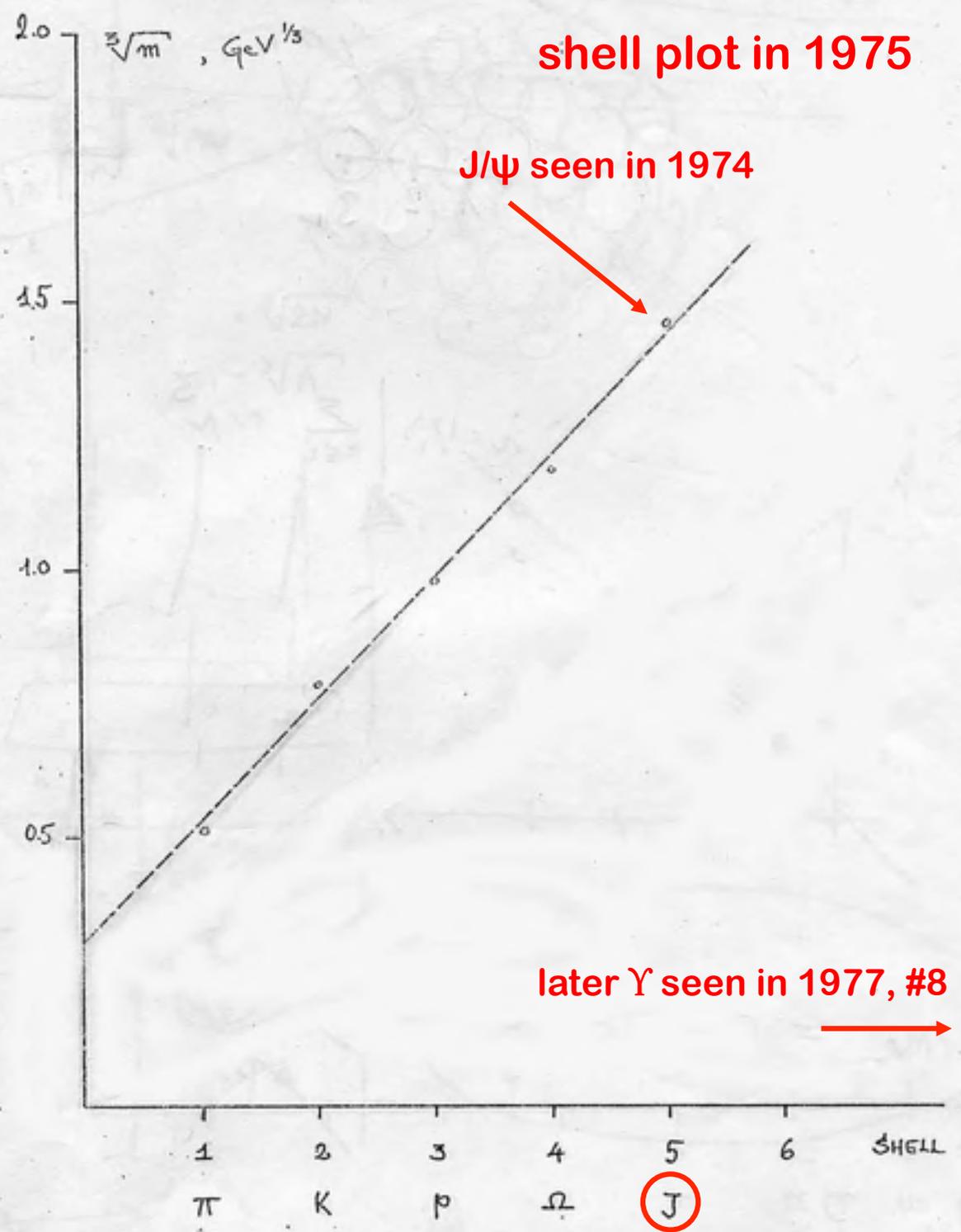
### RIASSUNTO

Un'ipotesi generale sul contributo dei componenti (sconosciuti) delle particelle alla massa totale, associata ad un semplice concetto geometrico di stabilità, implica che le radici cubiche delle masse delle particelle relativamente più stabili sono equispaziate.

La relazione suindicata è verificata sullo spettro di massa, e si predicono ulteriori zone di stabilità attorno a 4.6 GeV e 6.8 GeV .

Si stabilisce un' analogia con i nuclei ed i numeri magici.

Si traggono delle conclusioni sul numero dei componenti elementari del pione, e si formula l' ipotesi che i leptoni stabili siano i costituenti elementari della materia. Ne derivano alcune proprietà dell' interazione di legame, e conseguenze sul significato dei numeri quantici, in particolare il numero barionico.



I was not alone:

- mass difference of  $70 \text{ MeV}/c^2$ :
  - Nambu in 1952,
  - Mac Gregor in 1970, and a few others
- stable leptons as constituents:
  - Barut in 1979

Table I

Change of coupling constant from the simple formula (4) and (5).

Meson Kinetic Energy (Mev)	40	80	120	160	Coupling constant was taken $g_1=0.8g$ and the mass of $V^0$ particle to be $3000m_e$ . For $V^0 \rightarrow \pi^0 + \pi^0$ , we put $g_0 \approx g$ in (5), which is not sensitive to the value fixed.
$(g_{eff}^{normal}/g)^*$	0.52	0.40	0.28	0.17	
$(g_{eff}^{exchange}/g)^*$	1.32	1.39	1.46	1.51	

considerably in its magnitude, but the above simple arguments permits us to discuss roughly their angular distributions as follows; the normally scattered meson has angular distribution which is nearly the same as in reference 2, because the effect of  $V^0$ -particle is only to change the coupling constant. But as to the charge exchange scattering, the angular distribution is more like that of Process II, because this scattering is composed of process I and II and, exact evaluation shows that the process II is predominant<sup>1)</sup>. Since the angular distribution of scattered meson given in reference 2 is nearly the same for process I and II, and we may roughly expect almost the same angular distribution for normal- and exchange-scattering.

In conclusion, the writer wishes to express his sincere thanks to Prof. M. Kobayasi and to Mr. S. Takagi for their kind interest taken in this work.

- 1) For summary of references, see A. Pais, preprint.
- 2) J. Ashkin, A. Simon and R. E. Marshak, *Prog. Theor. Phys.* **5** (1950), 634.
- 3) P. J. Isaac, A. M. Sachs and J. Steinberger, *Phys. Rev.* **85** (1952), 803; *Fermi et al. Phys. Rev.* **85** (1952), 934, 935, 936.
- 4) Owing to the choice of coupling as given in Fig. 3, for  $\pi^+ + P^+ \rightarrow \pi^0 + N$ , we have as effective coupling constant, in (4) and (5)

$$g_{\pi^+ P^+}^2 = g_{\pi^+ N}^2 + \frac{[m_1 + m_2][(p_1 + q_1)^2 - m^2]}{2\omega[(p_0 + q_0)^2 - m_1^2]} g_1^2 g_{N_1}$$

$$g_{\pi^+ P^+}^2 = g_{\pi^+ N}^2 + \frac{[m_1 + m_2][(p_1 - q)^2 - m^2]}{2\omega[(p_0 - q)^2 - m_1^2]} g_1^2 g_{N_1}$$

$$= - \left( g_{\pi^+ N}^2 - \frac{[m_1 + m_2][(p_0 - q)^2 - m^2]}{2\omega[(p_0 - q)^2 - m_1^2]} g_1^2 g_{N_1} \right)$$

and thus,  $(g_{\pi^+ P^+}/g_{\pi^+ N})^2$  is just corresponding quantity in Table I,  $(g_{\pi^+ P^+}/g_{\pi^+ N})^2 = 0.8(g_{\pi^+ N}/g)^2$ , but  $(g_{\pi^+ P^+}/g_{\pi^+ N})^2$  is

40	80	120	160
0.72	0.67	0.62	0.59

**An Empirical Mass Spectrum of Elementary Particles**

Y. Nambu

Osaka City University

May 14, 1952

1952

It seems to be a general conviction of current physicists that the theory of elementary particles in its ultimate form could or should give the mass spectrum of these particles just in the same way as quantum mechanics has succeeded in accounting for the regularity of atomic spectra. Even if we disregard any philosophical background in such a postulation of theoretical physics, the recent discovery of many unstable, apparently elementary particles drives us in the efforts towards a systematic comprehension of the variety of elementary particles.

With the present undoubtedly insufficient accumulation of our knowledge, however, it may perhaps be too ambitious and rather unsound to look for an empirical "Balmer's law". Nevertheless we should like here to present one such attempt because it

$m_e/\alpha = 70.02 \text{ MeV}/c^2$

happens to be extremely simple, and because the significance and utility, if any, of this kind of attempt could best be appreciated at the stage where it awaits more experimental data to prove or disprove itself by its own predictions.

The nature of  $V_0$  particles<sup>1)</sup> and  $\tau$ -mesons<sup>2)</sup> has been investigated by several authors. Among other things, we note that their decay  $Q$ -values are rather uniform, i.e. of the same order of magnitude of the rest mass of the daughter  $\pi$ -mesons. This gives us a hint that some regularity might be found if the masses were measured in a unit of the order of the  $\pi$ -meson mass. The  $\pi$ -meson mass, being  $\sim 274 = 137 \times 2$  electron masses ( $m_e$ ), gives us a second, rather fanciful hint that  $137 m_e$  could be chosen as the unit. The ensuing result is given in the accompanying table. We see

particle	mass no. "n"	$137 \times n$	experimental mass
lepton	0	0	$\sim 0$
photon	0	0	0
$\mu$	$1\frac{1}{2}$	206	$210 \pm 3 m_e$
$\pi$	2	274	$276 \pm 3 (\pi^\pm)$
$V_{02}$	6	822	$800 \pm 30$
$\tau$	7	959	$966 \pm 10$
x			$1000 \sim 1500$
nucleon	$13\frac{1}{2}$	1849	1837, 1839
$V_{01}$	16, $16\frac{1}{2}$	$Q = 35, 70 \text{ Mev}$	$35 \pm 5, 75 \pm 3 \text{ Mev}$
$V^*$	$17\frac{1}{2}$	$Q = 280 \text{ Mev}$	$\sim 280 \text{ Mev}$

that the "mass number" of the observed particles is either integer or half-odd, which is generally valid within a deviation of about  $\sim \pm 15 m_e$ , or  $\sim \pm 1/10$  mass unit, for those cases in which the experimental error is also of this order of magnitude. In the above table, we have adopted the view that the heavy  $V_0$  particles have two kinds of  $Q$ -values, namely  $\sim 35 \text{ Mev}$  ( $1\frac{1}{2}$  mass unit) and  $\sim 70 \text{ Mev}$  ( $1 \text{ m.u.}$ )<sup>3)</sup>, decaying into a proton and a  $\pi$ -meson.  $V^*$  means the nucleon isobar whose existence is being con-

jectured from  $\gamma$ - $\pi$  reaction and  $\pi$ -proton scattering,<sup>5)</sup> with an excitation of roughly about 280 Mev (4 m.u.).

We can make a few comments on the result. ① As was pointed out by Enatsu<sup>4)</sup>, the adopted mass unit incidentally agrees with Heisenberg's natural unit. ② Bosons seem to have integral, while fermions half-integral, mass numbers. ③ The small mass value of the electron cannot be explained by the above rule. But we can take the view that this as well as the proton-neutron and  $\pi^\pm$ - $\pi^0$  mass differences correspond to a kind of fine structure. Indeed, their magnitude is just of the order of  $1/137$  m.u.

It goes without saying that this rule is purely of an empirical nature, and might turn out to be entirely illusory or accidental in the event of getting more reliable data or establishing the true theory of mass spectrum. But the rather strange distribution of the observed mass numbers might simply mean the lack of our knowledge. Indeed, only those particles which have favorable lives as well as abundances for detection have so far been observed, and we have no grounds at all to exclude the possibility that there exist other particles which are liable to escape direct observation. At any rate, an effective and close-by test of this rule may be provided by more accurate determination of the masses of the observed particles. In particular, the x-meson may be predicted to have any of  $\sim 1030, \sim 1100, \sim 1160, \sim 1230, \sim 1300, \dots$  electron masses ( $7\frac{1}{2}, 8, 8\frac{1}{2}, 9, 9\frac{1}{2}, \dots$  m.u.).

- 1) E. g., R. Armenteros et al., *Phil. Mag.* **42** (1951), 1113.
- 2) P. H. Fowler et al., *Phil. Mag.* **42** (1951), 1040.
- 3) S. D. Wanlass et al., *Bull. Amer. Phys. Soc.* **27** (1952), No. 3, 7.
- 4) Remarks by H. Enatsu at the Tokyo meeting of the Physical Society of Japan, April 1-3, 1952.
- 5) K. A. Brueckner, *Bull. Amer. Phys. Soc.* **27** (1952), No. 1, 50.

$$m_e/\alpha = 70.02 \text{ MeV}/c^2$$

### *Letters to the Editor*

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STABLE PARTICLES AS BUILDING BLOCKS OF MATTER \*

A.O. Barut \*\*

International Centre for Theoretical Physics, Trieste, Italy.

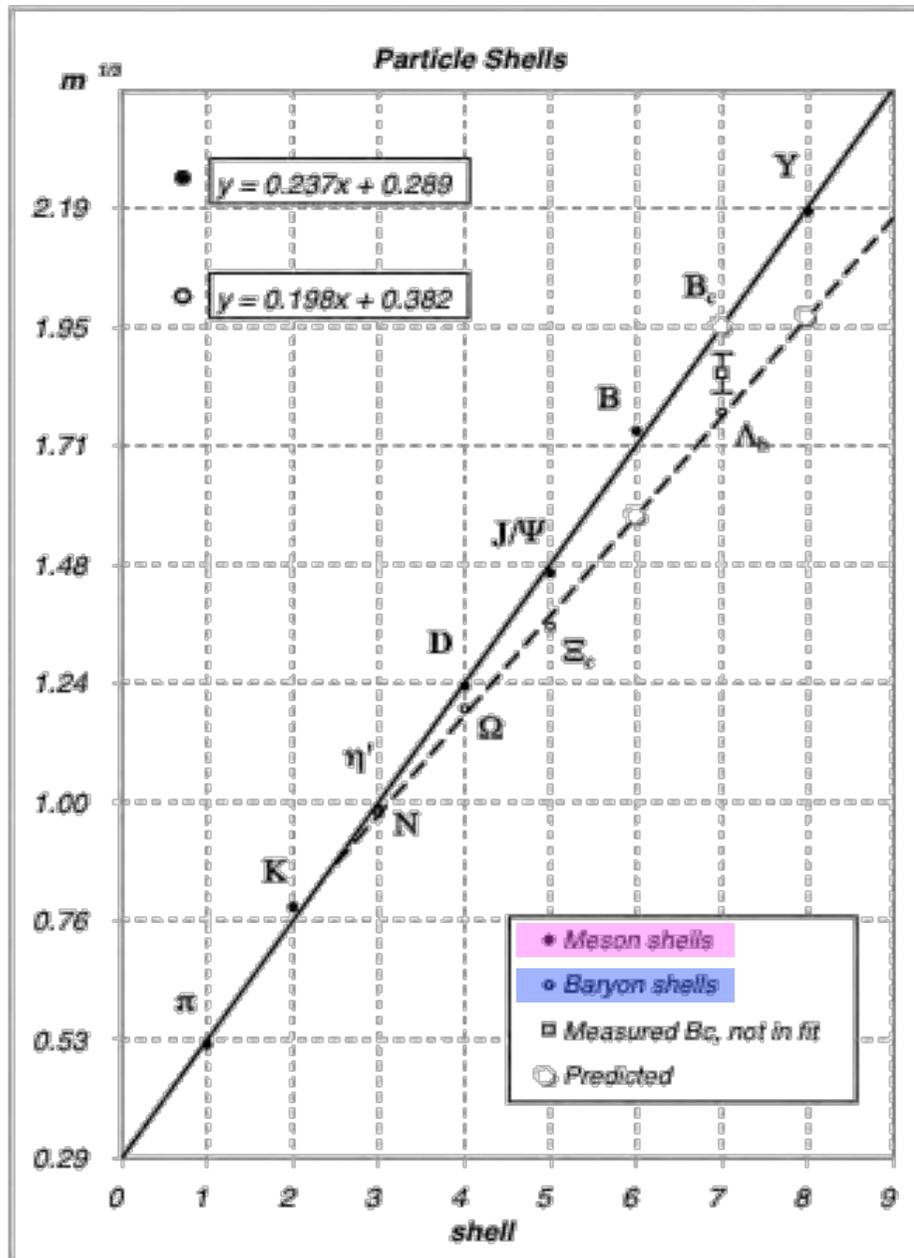
ABSTRACT

Only absolutely stable particles can be truly elementary. A simple theory of matter based on the three constituents, proton, electron and neutrino (and their antiparticles), bound together by the ordinary magnetic forces is presented, which allows us to give an intuitive picture of all processes of high-energy physics, including strong and weak interactions, and make quantitative predictions.

MIRAMARE - TRIESTE

April 1979

**~ 30 years later**



## Particles and Shells

Paolo Palazzi, CERN

### Abstract

The current understanding of particle masses in terms of quarks and their binding energy is not satisfactory. Both in atoms and in nuclei the organizing principle of stability is the shell structure, while this does not seem to play any role for particles. In order to explore the possibility that shells might also be relevant at this inner level of aggregation, atomic and nuclear stability are expressed by "stabilines", alignments of the 1/3 power of the total number of constituents of the most stable configurations. Could similar patterns be found in the particle spectrum? By analyzing the distribution of particle lifetimes as a function of mass, stability peaks are recognized for mesons and for baryons and indeed the cube roots of their masses follow two distinct stabilines. Such alignments would be a strong indication that the particles themselves are shell structured assuming only that each constituent contributes a constant amount to the total mass. This is incompatible with the prevalent view that the partons —real physical constituents seen in deep-inelastic scattering experiments—are the quarks. The mass of the  $B_c$  predicted by interpolation with the meson stabiline is  $7.4 \pm 0.2$  GeV. On the baryon stabiline two missing states are predicted at 3.9 and 7.6 GeV.

trouble...

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**must establish  
statistically relevant  
hadron mass rules!**

TABLES FROM UCRL-8030(rev. 1 June 1964)  
Table 5 - Stable particles

	$J^P(C_2)GA$	Mass (MeV)	Mass diff. (MeV)	Mean life (sec)	Mass <sup>2</sup> (BeV) <sup>2</sup>	Important decays		Q (MeV)	p or P <sub>exp</sub> (MeV)	
						Partial mode	Fraction			
$\gamma$	$1^-(0^-)C_2A$	0		stable	0	stable				
LEPTONS	$e^-$	$1^-(1/2^-)C_2A$	0 (<0.2 keV)	stable	0	stable				
	$\mu^-$	$1^-(1/2^-)C_2A$	0.511006 ± 0.000002	stable	0.000	stable				
	$\tau^-$	$1^-(1/2^-)C_2A$	105.659 ± 0.002	-13.95 ± 0.05	$2.2001 \times 10^{-6} \pm 0.0008$	0.011	evv	100%	105.45	52.
MESONS	$\pi^+$	$0^-(0^-)C_2A$	139.60 ± 0.05	-13.95 ± 0.05	$2.55 \times 10^{-8} \pm 0.26$	0.019	$\mu\nu$ $e\nu$ $\mu^+\nu$ $e^+\nu$	100% [5.244, 05]10 <sup>-9</sup> [1.244, 25]10 <sup>-9</sup> [1.5 a, 3]10 <sup>-8</sup>	33.95 139.40 33.94 4.08	29. 69. 29. 4.
	$\pi^0$	$0^-(0^-)C_2A$	135.01 ± 0.05	-4.590 ± 0.004	$1.80 \times 10^{-16} \pm 0.29$	0.018	$\gamma\gamma$ $\gamma^* \rightarrow e^+e^-$	98.8 [1.194, 05]%	135.01 133.99	67. 67.
	$K^+$	$1/2^+(0^-)A^-$	493.8 ± 0.2	-4.2 ± 0.5	$1.229 \times 10^{-8} \pm 0.008$	0.244	$\mu\nu$ $\pi^+\pi^0$ $\pi^+\pi^+\pi^-$	[63.14, 4]%, [21.54, 4]%, [5.54, 1]%	388.1 219.2 75.0	235. 205. 125.
	$K^0$	$1/2^+(0^-)A^-$	498.0 ± 0.5	-4.2 ± 0.5			For other decays see Table 5 Decays			
	$K_S^0$				$0.92 \times 10^{-10} \pm 0.02$	0.248	$\nu^+\nu^-$ $\pi^+\pi^0$	[69.945, 1]%, [30.641, 1]%	218.8 228.0	209. 209.
	$K_L^0$				$0.91 \times 10^{10} \pm 0.07$		$\pi^+\pi^-\pi^0$ $\pi^+\pi^-\pi^+\pi^-$ $\pi^+\pi^-\pi^0$	[27.143, 6]%, [12.7, 1.7]%, [26.643, 2]%	93.0 83.8 252.7	139. 133. 216.
	$K_S^*$				$4.65$	0.248	$\pi^+\pi^0$ $\pi^+\pi^-\pi^0$ $\pi^+\pi^-\pi^+\pi^-$	[33.643, 3]%	357.9	229.
	$\eta$	$0^-(0^-)C_2A$	548.7 ± 0.5		$\tau < 10$ MeV	0.301	$\gamma\gamma$ $3\pi^0$ or $\pi^+\pi^-\pi^0$ $\pi^+\pi^-\pi^+\pi^-$ $\pi^+\pi^-\pi^0$	[35.343, 0]%, [31.842, 3]%, [27.442, 3]%, [5.541, 3]%	548.7 143.7 134.5 269.5	274. 179. 174. 236.
	$\rho^+$	$1^-(1/2^-)$	938.256 ± 0.005	-1.2933	stable	0.860				
	$\rho^0$	$1^-(1/2^-)$	939.550 ± 0.005	-1.0001	$1.01 \times 10^{-3} \pm 0.03$	0.863	$\pi^+\pi^-$	100%	0.78	1.1
BARYONS	$\Delta^+$	$3/2^+(1/2^-)$	1155.40 ± 0.11		$2.6 \times 10^{-10} \pm 0.02$	1.244	$\pi^+\pi^0$ $\pi^+\pi^+\pi^-$ $\pi^+\pi^-\pi^0$	[61.741, 0]%, [31.642, 6]%, [13, 10] <sup>-4</sup>	31.5 40.9 71.5	100. 103. 130.
	$\Sigma^+$	$1/2^+(1/2^-)$	1189.41 ± 0.14	2.9	$0.786 \times 10^{-10} \pm 0.027$	1.415	$\pi^+\pi^0$ $\pi^+\pi^+\pi^-$	51.042, 4%, 49.042, 4%	116.13 110.26	189. 185.
	$\Sigma^0$	$1/2^+(1/2^-)$	1192.3 ± 0.3		$< 1.0 \times 10^{-14}$	1.422	$\Delta\gamma$	100%	77.0	74.
	$\Sigma^-$	$1/2^+(1/2^-)$	1197.08 ± 0.19	4.75 ± 0.10	$1.58 \times 10^{-10} \pm 0.05$	1.433	$\pi^-\pi^0$	100%	116.94	191.
	$\Sigma^*$	$3/2^+(1/2^-)$	1114.3 ± 1.0	6.5 ± 1.0	$3.06 \times 10^{-10} \pm 0.40$	1.727	$\Delta\pi^0$	100%	76.9	150.
	$\Sigma^{*-}$	$3/2^+(1/2^-)$	1120.8 ± 0.2		$1.74 \times 10^{-10} \pm 0.05$	1.745	$\Delta\pi^-$ $\Delta e^+\nu$ $\pi^-\pi^0$	100% [3.041, 7]10 <sup>-3</sup> $< 5 \times 10^{-3}$	65.8 204.9 214.2	138. 169. 303.
$\Sigma^{*-}$	$3/2^+(1/2^-)$	1675 ± 3		$-0.7 \times 10^{-10}$		$\Sigma^0$ $\Delta K$	? ?	221 66	296 216.	

A. H. Rosenfeld, A. Barbaro-Galtieri, W. H. Barkas, P. L. Bastien, J. Kirz, M. Roos  
UCRL-8030 - Part I, June 1964.

The Nobel Prize in Physics 2004 - Information for the Public

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**The Nobel Prize in Physics 2004 - information for the Public**  
5 October 2004

The discovery which is awarded this year's Nobel Prize is of decisive importance for our understanding of how the theory of one of Nature's fundamental forces works, the force that ties together the smallest pieces of matter - the quarks. **David Gross, David Politzer and Frank Wilczek** have through their theoretical contributions made it possible to complete the Standard Model of Pa objects in Nature and how they interact in the endeavour to provide a unified picture of the spatial scale - from the tiniest distances of the universe.

**The strong force explained**

The strong interaction - often called the force that binds the nucleons together - acts between the quarks, the building blocks of nuclei. Progress in particle physics or nuclear physics may appear hard to grasp for anyone with no background in physics, but it is in fact determined by the fundamental forces of nature: the strong force, the electromagnetic force, the weak force and gravity. In fact, about 80% of the energy in the interior of the proton and neutron is due to the strong force. This year's Nobel Prize is about this interaction.

**David Gross, David Politzer and Frank Wilczek** have through their theoretical contributions made it possible to complete the Standard Model of particle physics and how they interact in the endeavour to provide a unified picture of the spatial scale - from the tiniest distances of the universe.

The strong interaction which explains why quarks are bound together into protons and neutrons. The discovery laid the foundation for a more complete name is Quantum Chromodynamics (QCD). The discovery was made in great detail, in particular during recent years at the Large Hadron Collider (LHC) at CERN, in Geneva.

# atomic physics timeline

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## CHEMISTRY

1808 Dalton: chemistry is atomic

## TAXONOMY

1869 Mendeleev: periodic table

## ENERGY LEVELS

1885 Balmer: spectral rules

1890 Rydberg: extended spectral rules

## CONSTITUENTS

1897 Thomson: electron

## MODEL

1907 Lenard: model with (+,-) charges

1904 Nagaoka: planetary model

1913 Bohr: model of the H atom

## THEORY

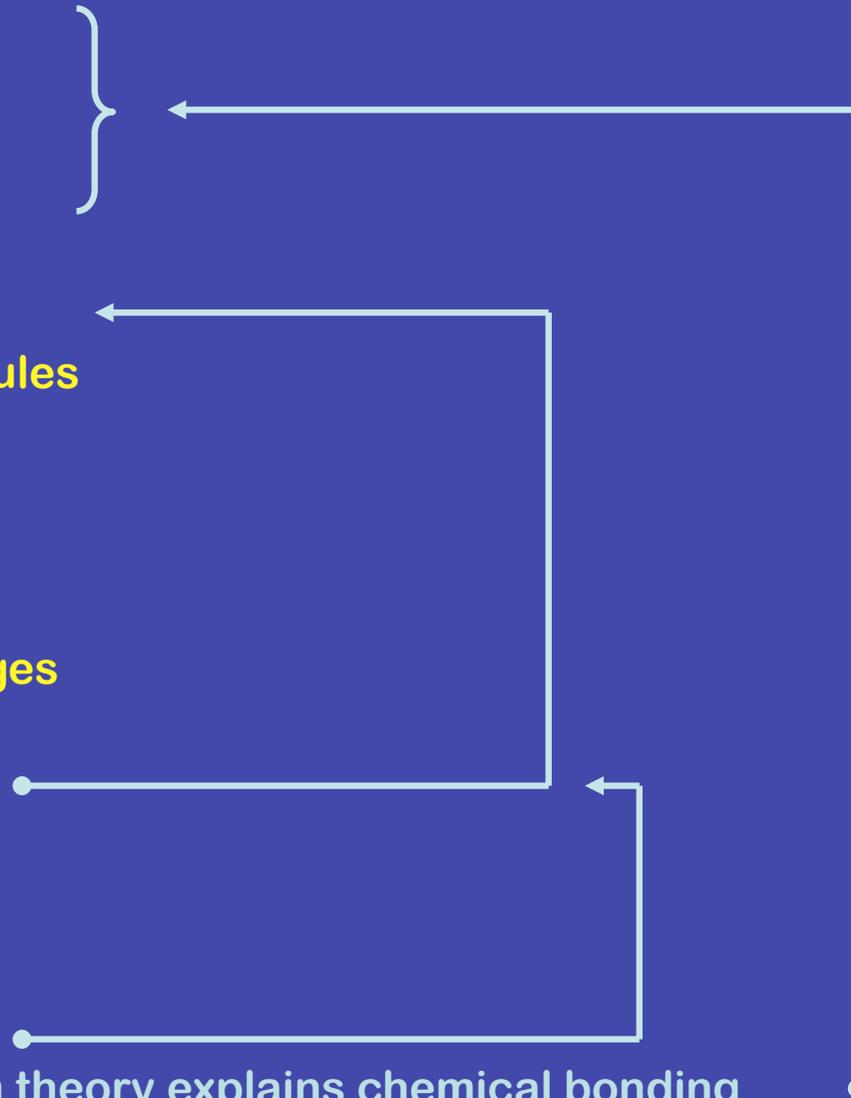
1925 Heisenberg: matrix (QM)

1926 Schroedinger: equation (QM)

1926 Schroedinger: H atom

1927: Heitler and London, quantum theory explains chemical bonding

1928 Dirac: equation



# particle physics timeline

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## TAXONOMY

1961 SU(X) multiplets: plausible but incomplete

## ENERGY LEVELS (MASSES)

lots of data, but no rules:

1962-64 GMO and 1962 Chew-Frauschi plot,  
no longer quoted by the PDG

## CHEMISTRY

1963 Cabibbo: later re-expressed as quark mixing, later CKM

## MODEL

1964 quark "model" evolved from taxonomy, schematic

???

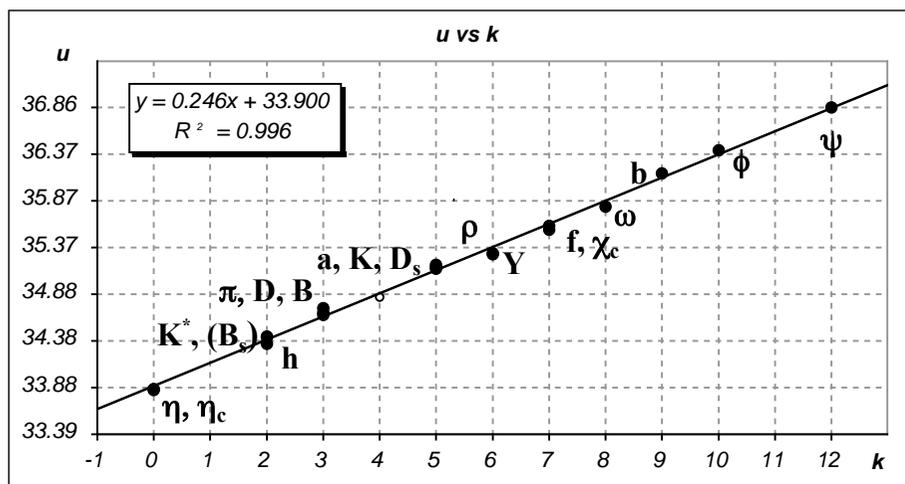
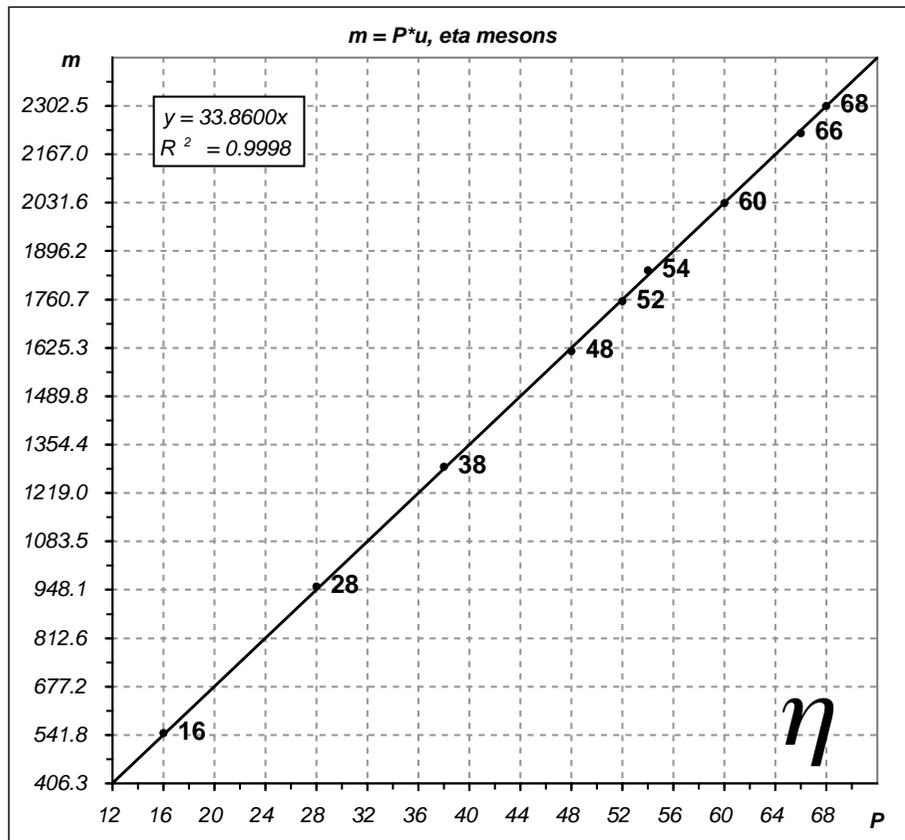
## CONSTITUENTS

1969 partons (.. = quarks, undeconfined)

## THEORY

197x, blessed in 2004: perfect, but ...

**the meson mass system**



# Patterns in the Meson Mass Spectrum

Paolo Palazzi 2004

## Abstract

The conjecture that particle masses are multiples of a unit  $u$  of about 35 MeV has been proposed in various forms by several authors: mesons are even multiples of  $u$ , leptons and baryons odd multiples. Here this mass quantization is reassessed for all particles with mass below 1 GeV (stable leptons and  $f_0(600)$  excluded), and found to be statistically significant. Subsequently all the mesons listed by the PDG are grouped in families defined by quark composition and  $J^{PC}$ , and analyzed for even mass multiplicity with a unit close to 35 MeV separately for each group. For all the families that can be analyzed unambiguously this multiplicity hypothesis is found to be statistically significant. Most scalar and vector families show a dependence of  $u$  from the spin, while for pseudoscalars the effect is not present. Only 5 states out of 120 are rejected due to abnormally large fit residuals. The mass units of the various families are quantized on a grid of 12 intervals of about 0.25 MeV, ranging from 33.88 up to 36.86 MeV. The location of the values on the  $u$ -grid shows an intriguing pattern of correlation with the quantum numbers.

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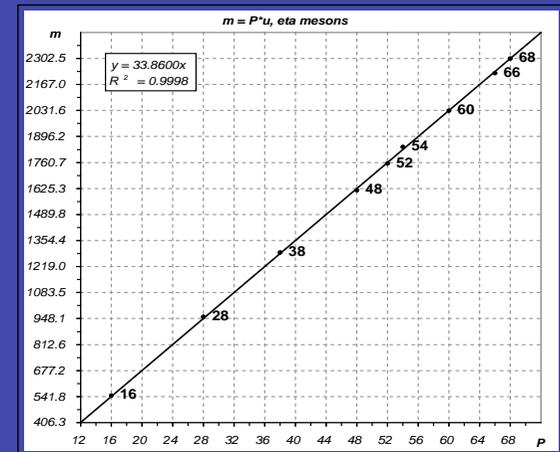
# NB: two kinds of plots

- mass unit:  
mass vs integer: linear-linear

$m$  vs  $P$

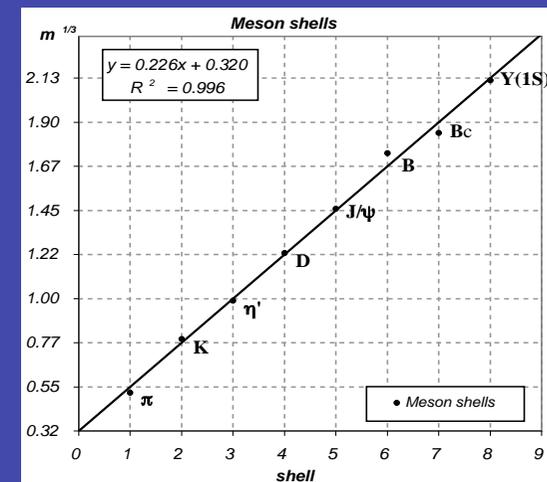
(also mass unit vs integer)

$u$  vs  $k$



- shells:  
 $X^{1/3}$  vs integer: cuberoot-linear

$m^{1/3}$  vs  $i_s$



mass unit:  $u \cong 35 \text{ MeV}/c^2$  to avoid half-integers

hypothesis:

$$m_i = u * P_i : P \in E \text{ for mesons}$$

$(P \in O \text{ for baryons and leptons})$

test procedure:

FOREACH set of [mesons / (q-qbar,  $J^{PC}$ )] DO:

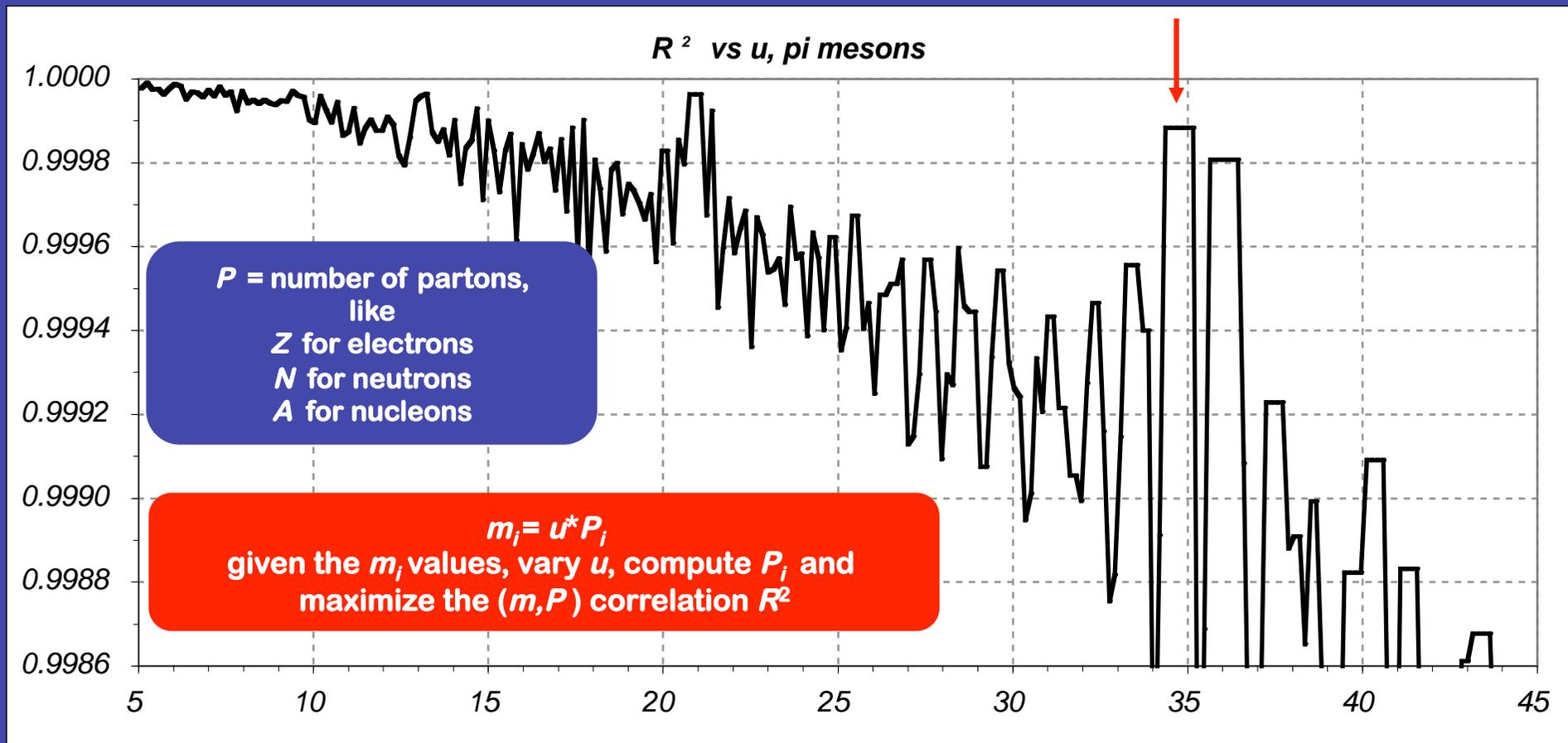
1. discard states with large  $errm$
2. maximize  $R^2(m, P)$  varying  $u$  around  $35 \text{ MeV}/c^2$
3. fit  $u$  with the least squares
4. remove outliers with Chauvenet's criterion
5. check for spin dependence  $du / dJ$
6. compute statistical relevance as  $p(H_0)$  by MC

ENDDO

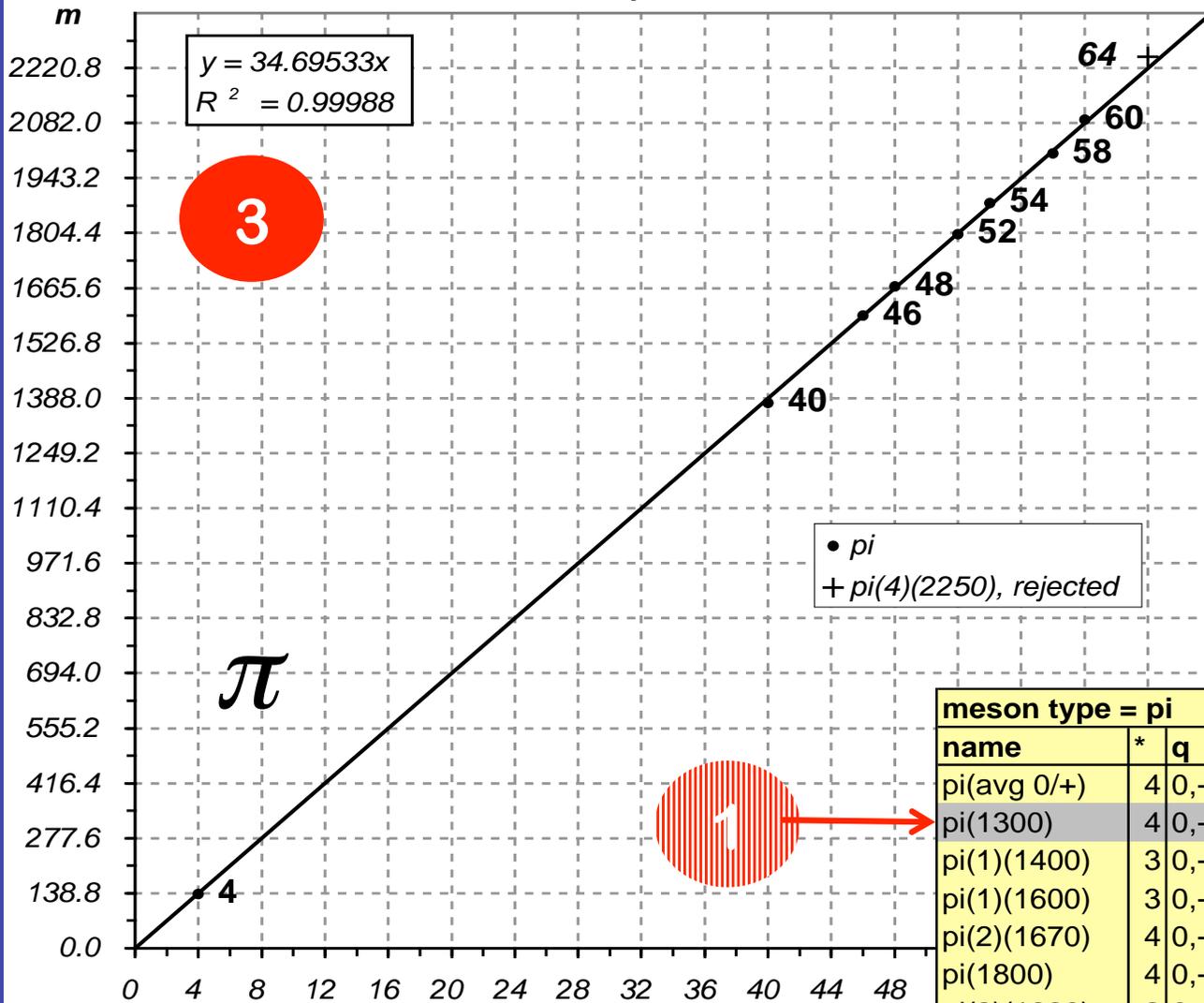
# example: the pions

1 remove states with large errors

2 maximize  $R^2$  varying  $u$



$m = P \cdot u$ , pions



residuals,  
compare with  
[-34.7, 34.7]  
uniform

meson type = pi										
name	*	q	J	x	P	m	errm	u=m/P	dm	dm/m
pi(avg 0/+)	4	0,+	0		4	137.3	6.0E-04	34.318	-1.8	1.33%
pi(1300)	4	0,+	0	1	38	1300.0	100.0	34.211	-18.4	1.42%
pi(1)(1400)	3	0,+	1		40	1376.0	17.0	34.400	-14.9	1.09%
pi(1)(1600)	3	0,+	1		46	1596.0	20.0	34.696	-3.6	0.22%
pi(2)(1670)	4	0,+	2		48	1670.0	20.0	34.792	0.9	0.05%
pi(1800)	4	0,+	0		52	1801.0	13.0	34.635	-7.2	0.40%
pi(2)(1880)	2	0,+	2		54	1880.0	20.0	34.815	2.2	0.12%
pi(2)(2005)	2	0,+	2		58	2005.0	15.0	34.569	-11.9	0.59%
pi(2)(2100)	3	0,+	2		60	2090.0	29.0	34.833	3.6	0.17%
pi(4)(2250)	2	0,+	4	3	64	2250.0	15.0	35.156	24.5	1.09%

4 →

5 →

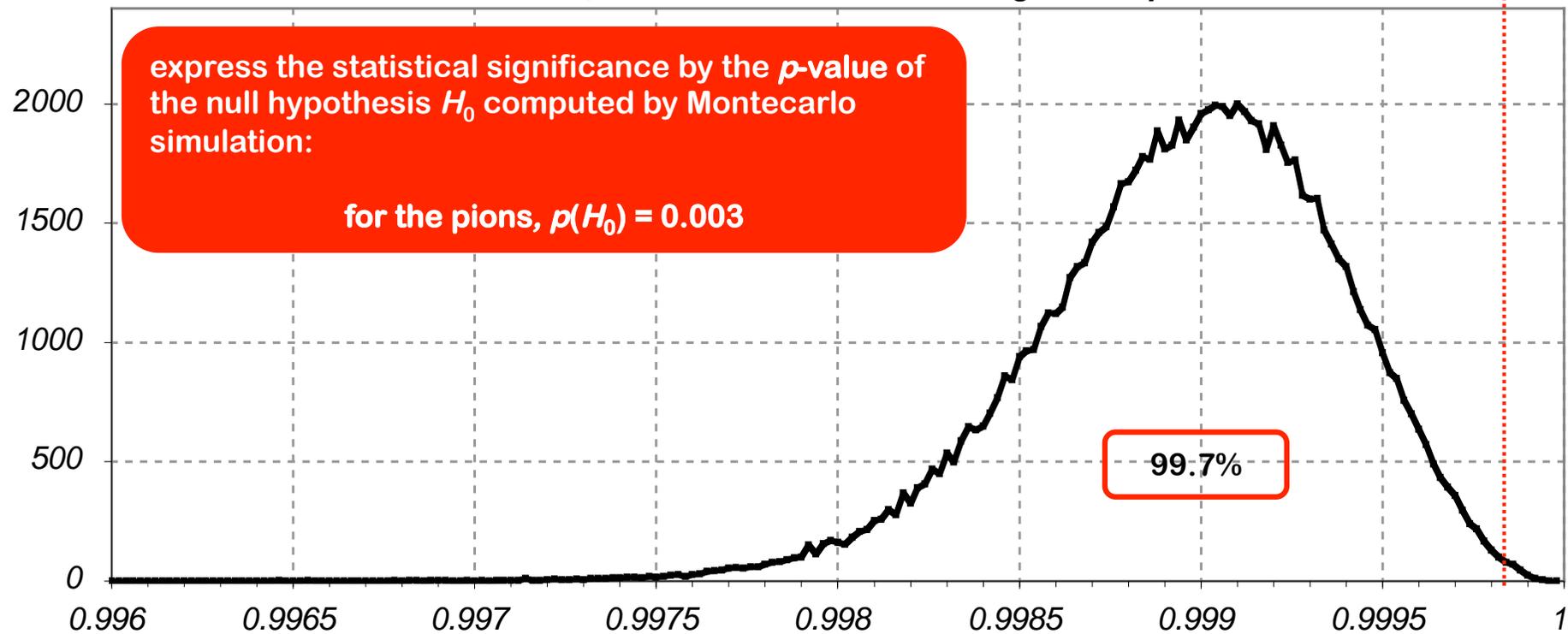
summary pi mesons	
u	$34.69 \pm 0.051$
p-value	0.997 --> $p(H_0) = 0.003$
spin dependence	no
omitted	3 = 1 averaged + 1 large erm + 1 Chauvenet

## 6

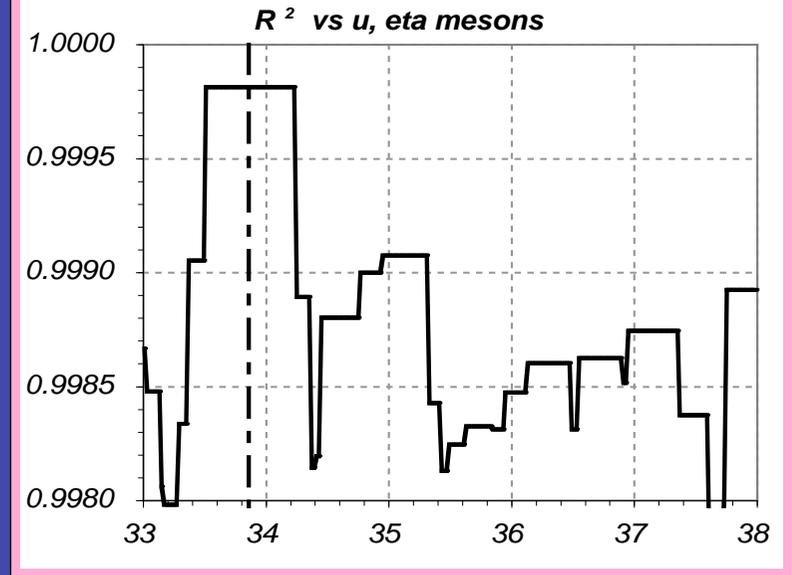
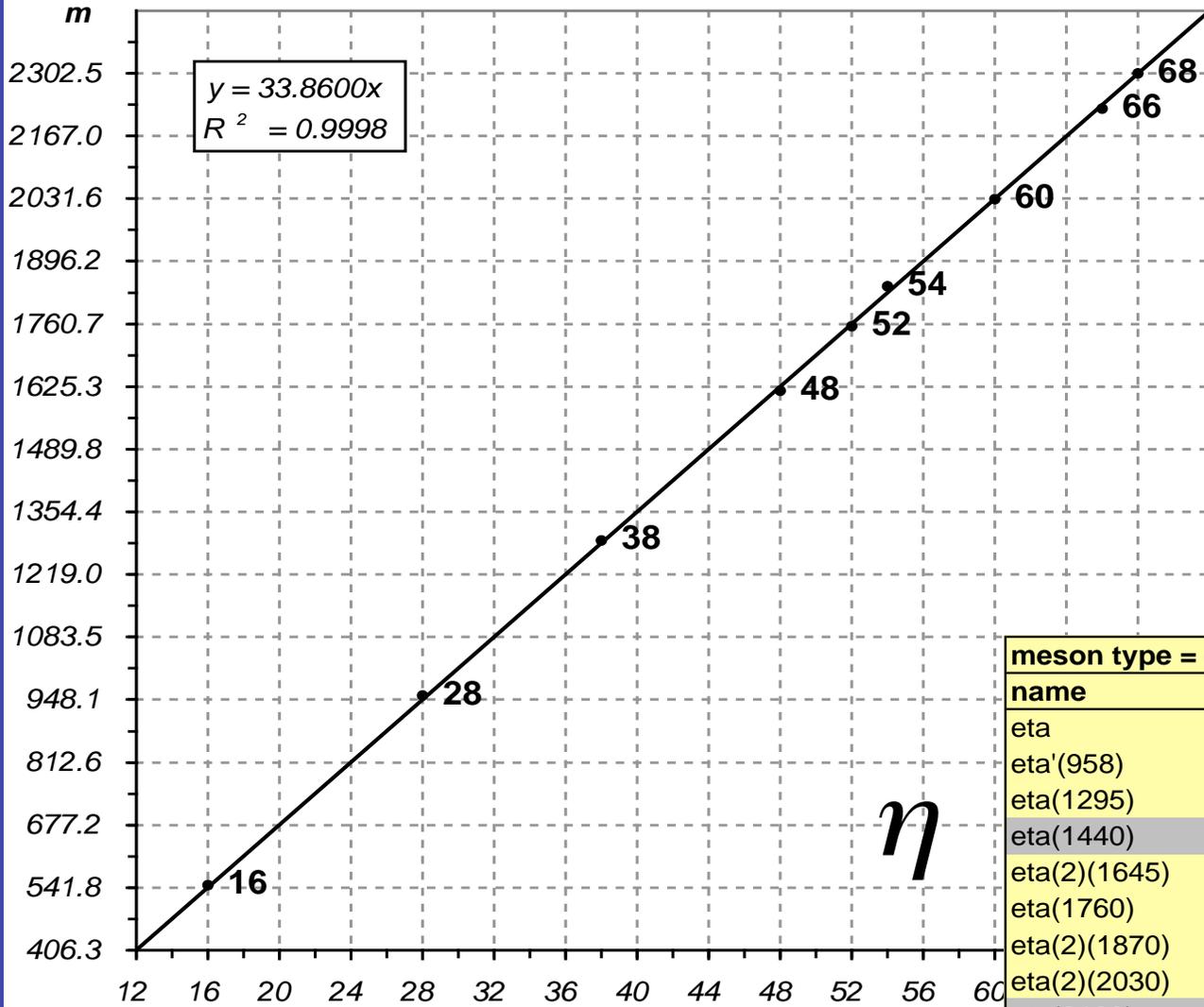
## statistical relevance

$$R^2 = 0.99988$$

$R^2$  distribution, 8 random masses in the range of the pions



$m = P \cdot u$ , eta mesons



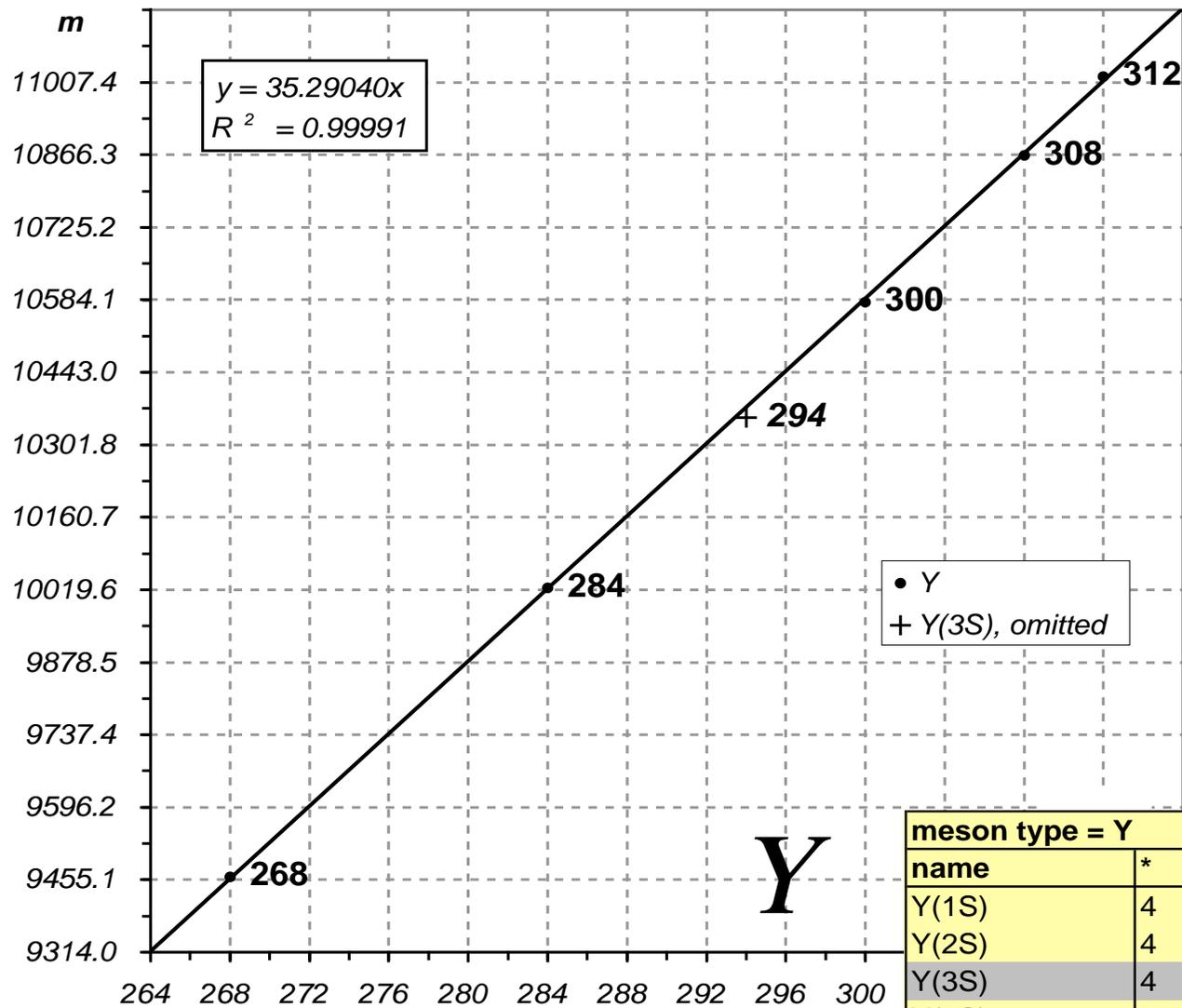
residuals

meson type = eta										
name	*	q	J	x	P	m	errm	u=m/P	dm	dm/m
eta	4	0	0		16	547.3	0.1	34.206	5.5	1.01%
eta'(958)	4	0	0		28	957.8	0.1	34.206	9.7	1.01%
eta(1295)	4	0	0		38	1293.0	5.0	34.026	6.3	0.49%
eta(1440)	4	0	0	1	42	1435.0	35.0	34.167	12.9	0.90%
eta(2)(1645)	3	0	2		48	1617.0	5.0	33.688	-8.3	-0.51%
eta(1760)	3	0	0		52	1756.0	11.0	33.769	-4.7	-0.27%
eta(2)(1870)	3	0	2		54	1842.0	8.0	34.111	13.6	0.74%
eta(2)(2030)	2	0	2		60	2030.0	20.0	33.833	-1.6	-0.08%
eta(2190)	2	0	0	1	64	2190.0	50.0	34.219	23.0	1.05%
eta(2)(2250)	2	0	2		66	2225.8	13.0	33.723	-9.0	-0.40%
eta(2225)	3	0	0	1	66	2227.0	35.0	33.742	-7.8	-0.35%
eta(2280)	3	0	0		68	2302.5	12.0	33.860	0.0	0.00%
eta(4)(2320)	2	0	4	1	68	2328.0	38.0	34.235	25.5	1.10%

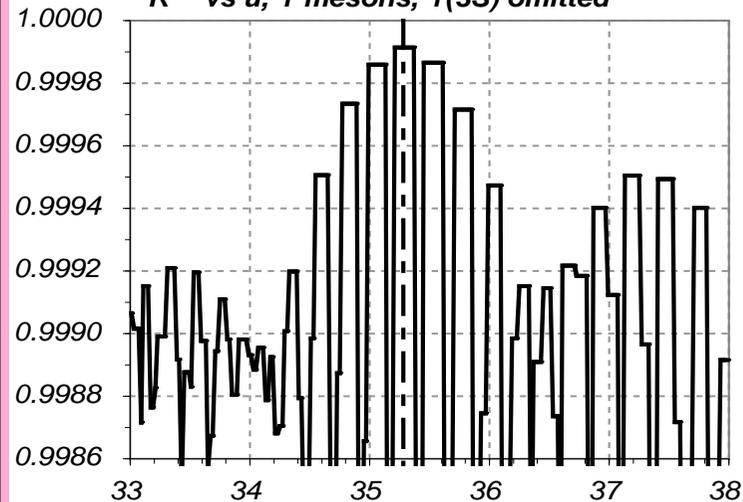
summary eta mesons	
u	33.86 ± 0.053
p-value	0.999 --> $p(H_0) = 0.001$
spin dependence	no
omitted	4 large errm

low mass

$m = P \cdot u$ , Y mesons



$R^2$  vs u, Y mesons, Y(3S) omitted

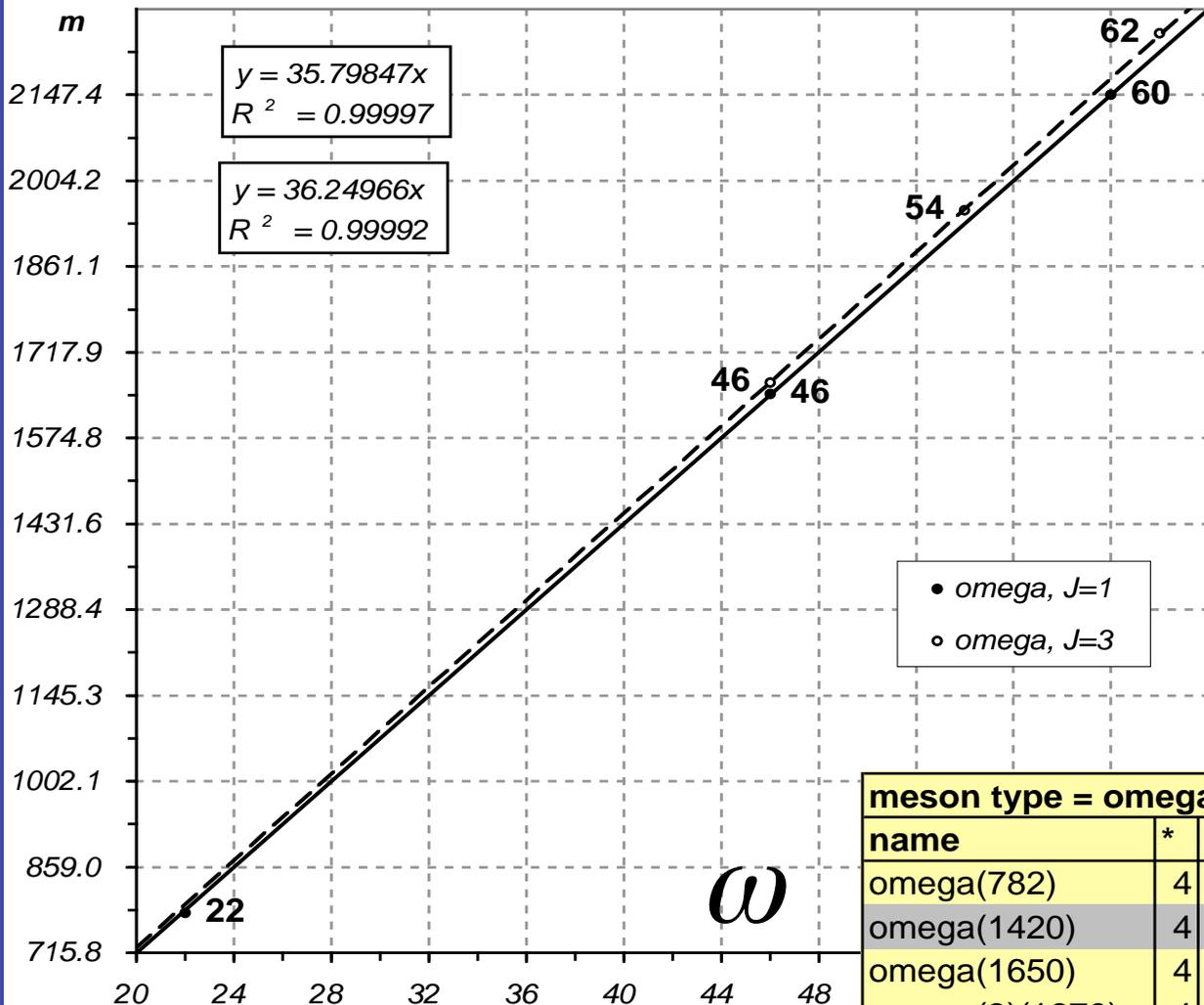


meson type = Y										
name	*	q	J	x	P	m	errm	u=m/P	dm	dm/m
Y(1S)	4	0	1		268	9460.3	0.26	35.300	5.5	0.06%
Y(2S)	4	0	1		284	10023.3	0.31	35.293	4.0	0.04%
Y(3S)	4	0	1	3	294	10355.2	0.50	35.222	-16.8	-0.16%
Y(4S)	4	0	1		300	10580.0	3.50	35.267	-3.7	-0.04%
Y(10860)	4	0	1		308	10865.0	8.00	35.276	-0.9	-0.01%
Y(11020)	4	0	1		312	11019.0	8.00	35.317	11.9	0.11%

summary Y mesons	
u	$35.29 \pm 0.009$
p-value	0.985 $\rightarrow p(H_0) = 0.015$
spin dependence	not assessed, all states are J=1
omitted	1 Chauvenet

high mass

$m = P \cdot u$ , omega mesons



meson type = omega										
name	*	q	J	x	P	m	errm	u=m/P	dm	dm/m
omega(782)	4	0	1		22	782.6	0.1	35.571	-5.0	-0.64%
omega(1420)	4	0	1	1	40	1419.0	31.0	35.475	-12.9	-0.91%
omega(1650)	4	0	1		46	1649.0	24.0	35.848	2.3	0.14%
omega(3)(1670)	4	0	3		46	1667.0	4.0	36.239	-0.5	-0.03%
omega(3)(1995)	2	0	3		54	1955.0	30.0	36.204	-2.5	-0.13%
omega(2145)	2	0	1		60	2148.0	15.0	35.800	0.1	0.00%
omega(3)(2250)	2	0	3		62	2250.0	20.0	36.290	2.5	0.11%

spin dependence  
du/dJ

summary omega mesons	
omitted	1 large errm
spin dependence	yes, Z=13.9
u, J=1	35.80 ± 0.049
p-value	> 0.934 (all states), 0.942 for J=1, 0.947 for J=3

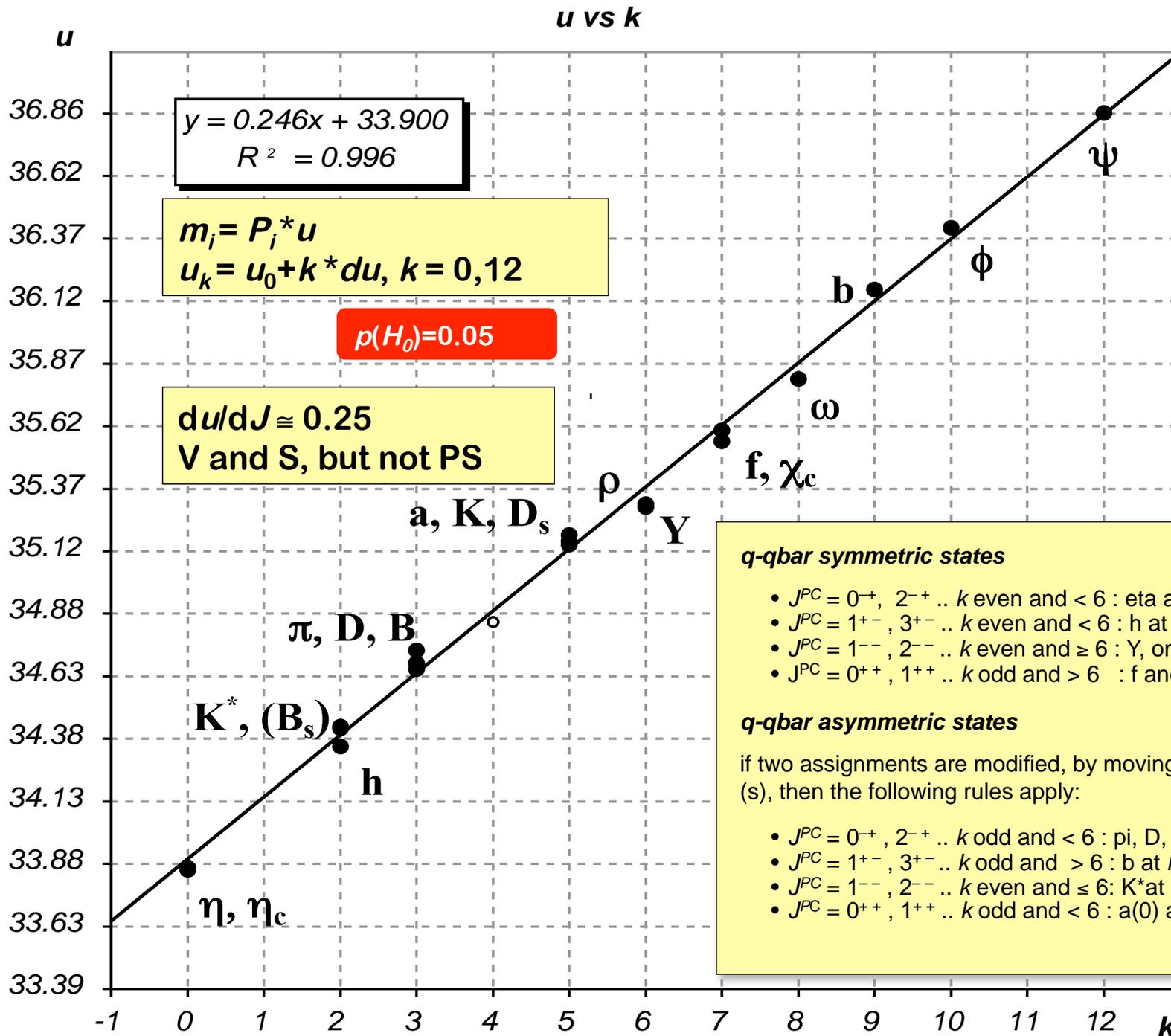
# summary

## Summary of mass unit analysis, mesons

type	k	u	erru	uw	p-value	du/dJ	states	omitted				used	rating	
							PDG	(1)	(2)	(3)	(4)	tot		
<b>pi</b>	<b>3</b>	34.69	0.051	34.68	0.997	N	11	1		1	1	3	8	****
<b>b</b>	<b>9</b>	36.16	0.050	36.16	0.990	N	3						3	***
<b>rho</b>	<b>6</b>	35.19	0.071	<b>35.31</b>	0.973	N	11	2		1		3	8	***
<b>a</b>					0.995	Y	13	2				2	11	****
<b>a(0)</b>	<b>5</b>	35.00	0.073	<b>35.17</b>	0.941									
<b>K</b>	<b>6</b>	35.34	0.073	35.39	0.943	N	11				1	1	10	***
<b>K*</b>					0.882	Y	12	1		1	2	4	8	
<b>K*(1)</b>	<b>2</b>	34.35	0.016	34.35										****
<b>eta</b>	<b>0</b>	33.86	0.053	33.86	0.999	N	13	4				4	9	****
<b>h</b>	<b>2</b>	34.42	0.056	34.43	0.975	N	6	2				2	4	****
<b>omega</b>					0.934	Y	7	1				1	6	****
<b>omega(1)</b>	<b>8</b>	35.80	0.049	35.81	0.943									
<b>phi</b>					0.732	Y	3						3	**
<b>phi(1)</b>	<b>10</b>	36.51	0.050	<b>36.41</b>										
<b>f</b>	<b>7</b>	35.78	0.070	<b>35.60</b>	0.998	?	33	5	18			23	10	***
<b>D<sup>+</sup></b>	<b>3</b>	34.67	0.016	34.66	0.997	N	5						5	****
<b>D<sup>0</sup></b>		34.58	0.023	34.60	0.960	N	4						4	****
<b>D(s)</b>	<b>5</b>	35.16	0.021	35.15	0.997	N	6						6	****
<b>eta(c)</b>	<b>0</b>	33.89	0.022	33.87			2						2	**
<b>psi</b>	<b>12</b>	36.84	0.034	36.87	0.959		7			1		1	6	****
<b>chi(c)</b>	<b>7</b>	35.57	0.006	35.56		Y	3						3	**
<b>B</b>	<b>3</b>	34.74	0.005	34.73			3				1	1	2	*
<b>B(s)</b>	<b>2</b>	34.42	0.004	34.42			2						2	*
<b>Y</b>	<b>6</b>	35.29	0.009	35.30	0.985		6			1		1	5	****
<b>avg-&gt;</b>			0.044		0.949		161	18	18	<b>5</b>	5	46	115	<b>&lt;-tot</b>
leptons	<b>4</b>	34.84	0.022	34.84			2						2	**

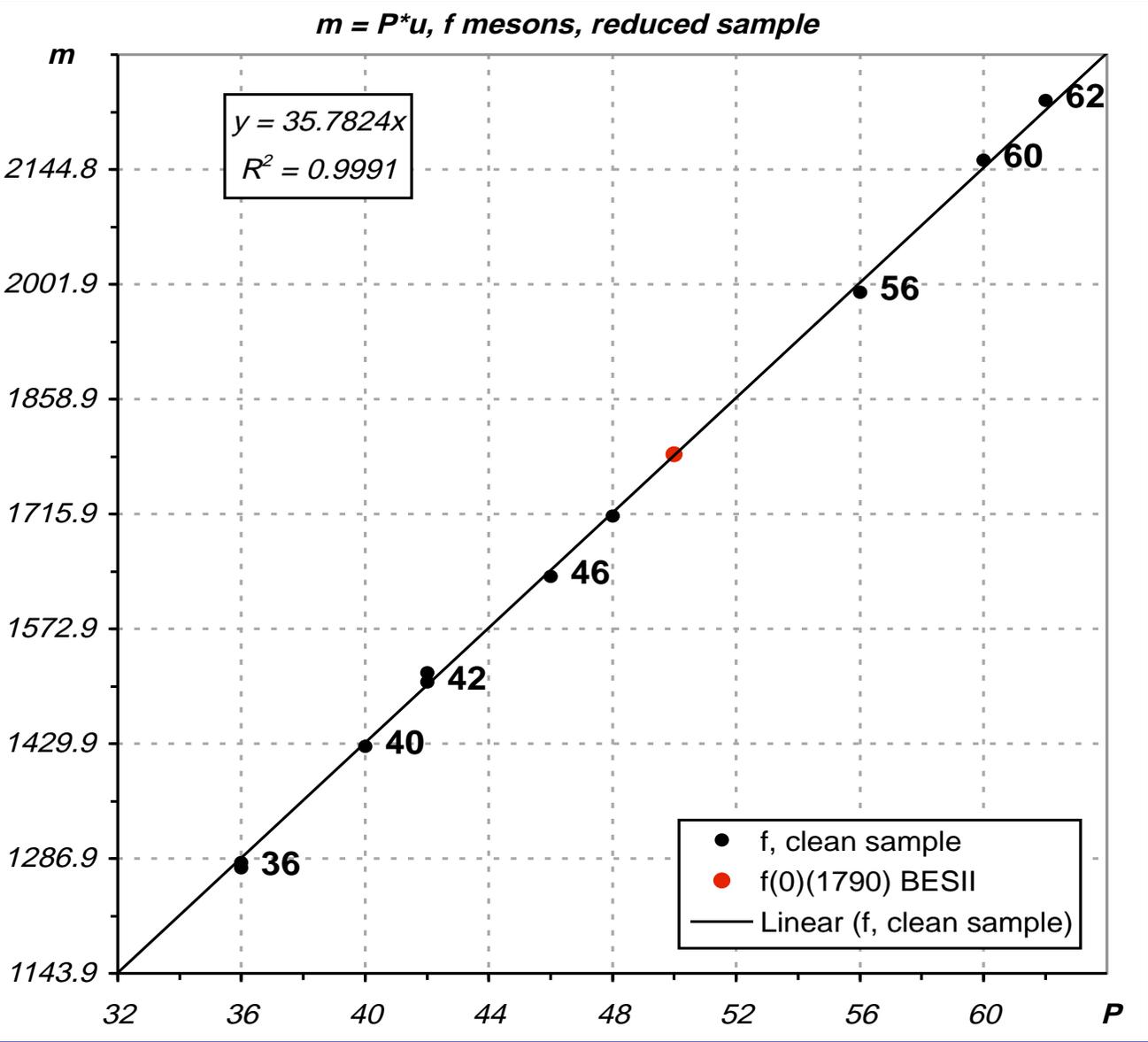
# u-quantum

du/dk

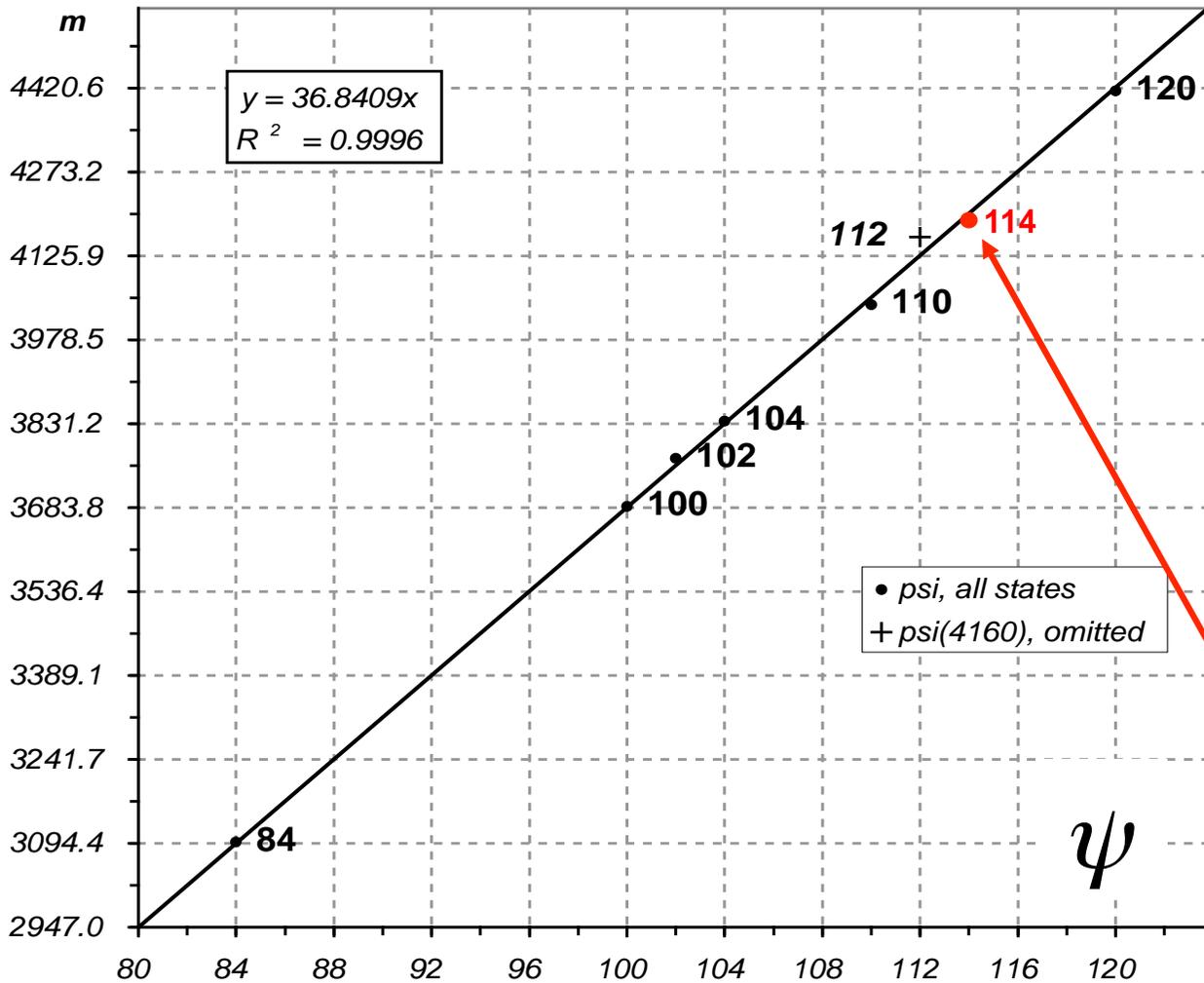


**predictions**

# new states must agree (and they do)



$m = P \cdot u$ , psi mesons



Reject: psi(4160)

2004: psi(4160) rejected

The psi(4160) with a residual of 33, rejected by Chauvenet's criterion. Its mass quoted by the PDG is based on a single measurement by DASP, and in the DASP paper the result of their analysis is compared with MARK1 data showing a more complex peak structure.

Above the psi(4040) the MARK1 data show a peak at around 4110 and possibly more. The psi(4415) is seen unambiguously by both experiments. The DASP view of the discrepancy is: "...our data are in closer agreement with those of SLAC-LBL but show some differences in the finer details of the energy dependence. For instance the 4.16 structure is not resolved in the SLAC-LBL data".

For sure there are differences, but the DASP interpretation is questionable. Apparently some MARK1 peaks were never identified or never made it to the PDG. A possible interpretation of their spectrum around 4100 is: psi(4040), P=110; psi(4125), P=112; possibly a psi(4200), P=114; no psi(4160).

2007: new BES value = 4191.6 ± 6.0

outliers

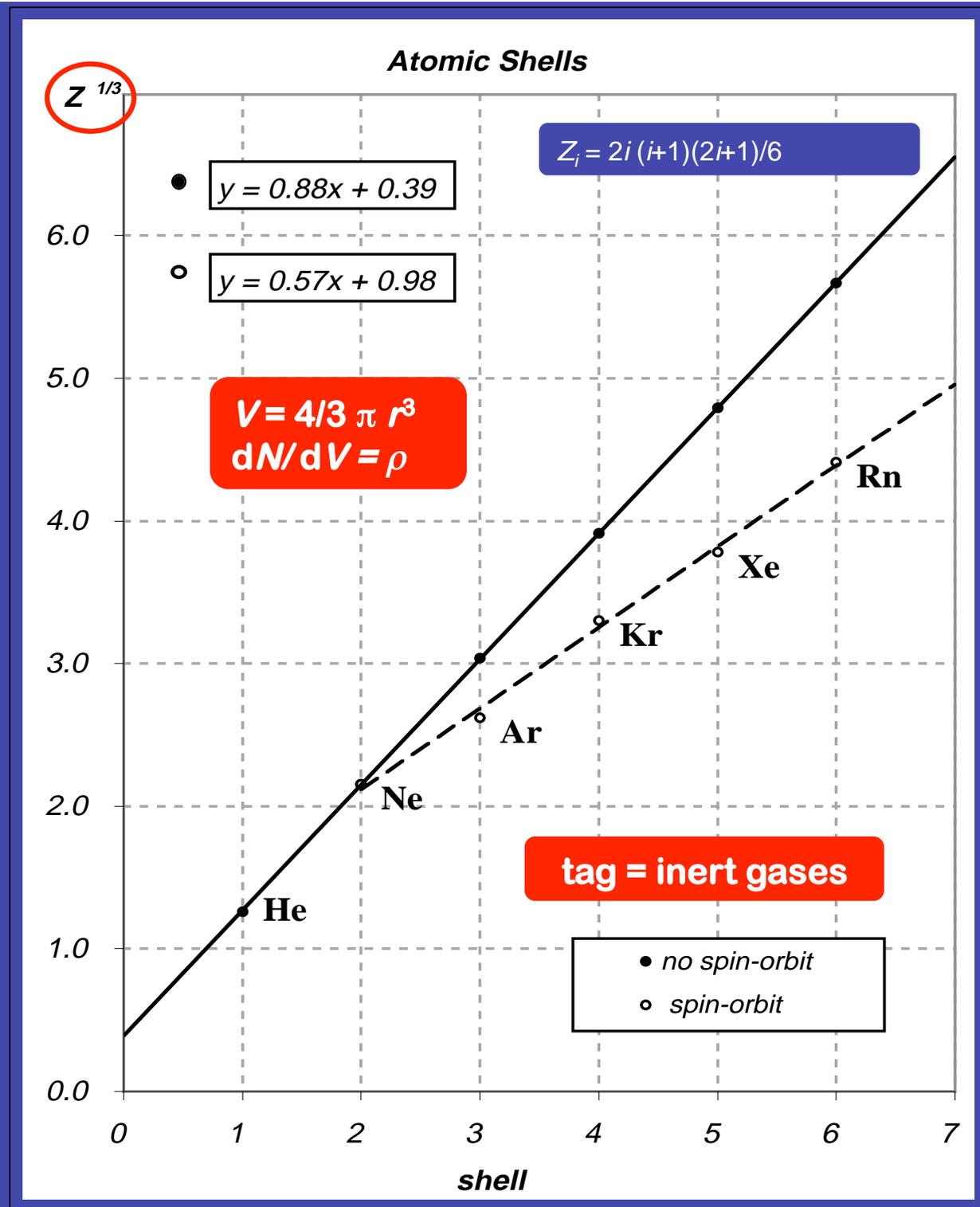
meson type = psi

name	*	q	J	x	P	m	errm	u	dm	dm/m
psi(1S)	4	0	1		84	3096.9	4.0E-02	36.868	2.2	0.07%
psi(2S)	4	0	1		100	3686.0	9.0E-02	36.860	1.9	0.05%
psi(3770)	4	0	1		102	3769.9	2.5	36.960	12.1	0.32%
psi(3836)	3	0	2?		104	3836.0	13.0	36.885	4.5	0.12%
psi(4040)	4	0	1		110	4040.0	10.0	36.727	-12.5	-0.31%
psi(4415)	4	0	1		120	4415.0	6.0	36.792	-5.9	-0.13%
psi(4160)	4?	0	1	3	112	4159.0	20.0	37.134	32.8	0.79%

**back to meson shells**

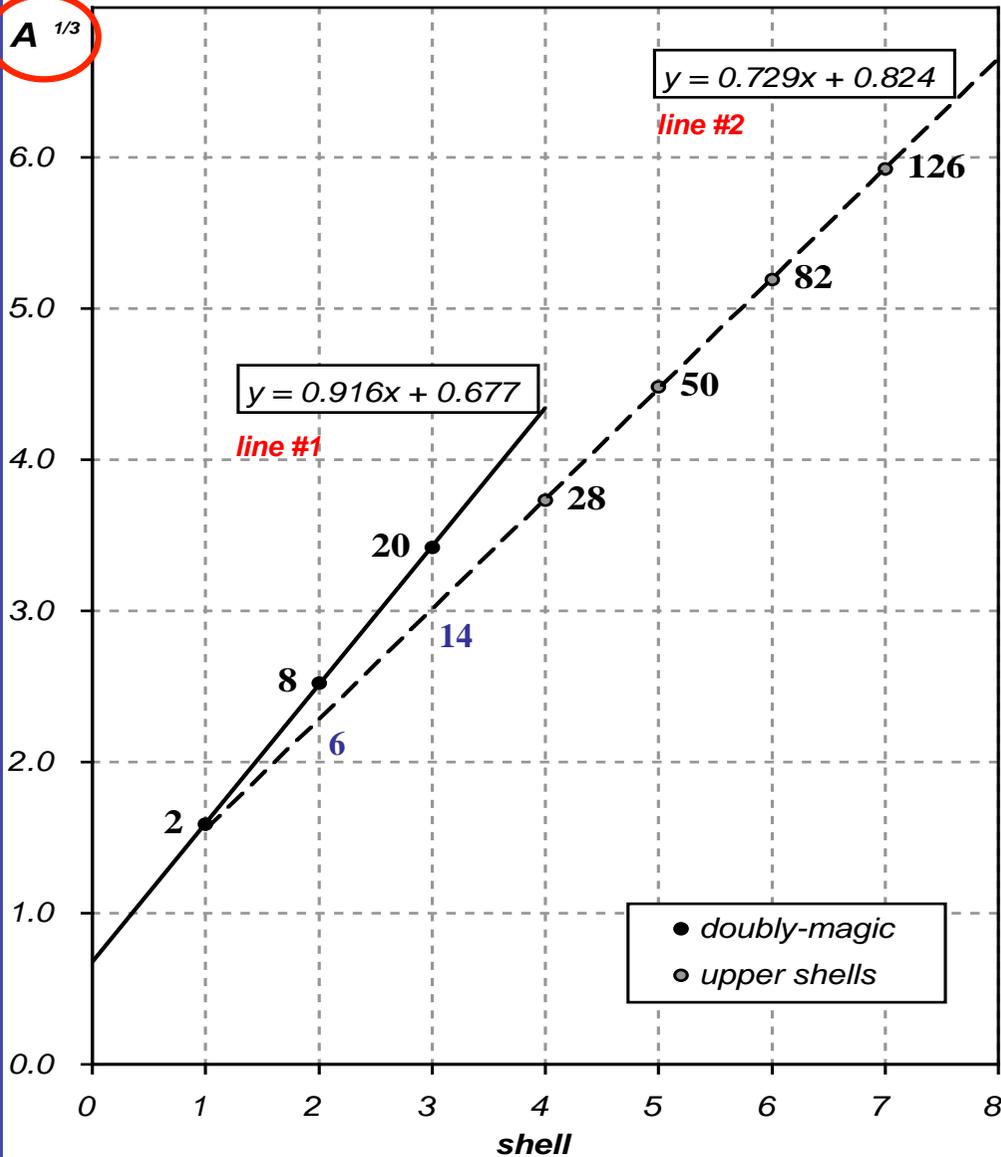
# atomic shells

$Z^{1/3}$



## Nuclear shells

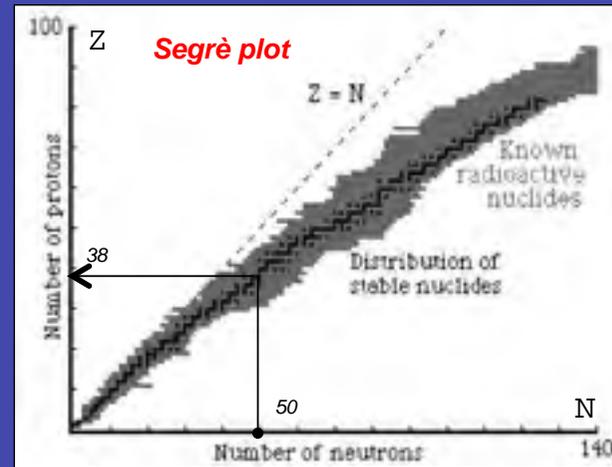
$A^{1/3}$



$N_i = 2, 8, 20, 28, 50, 82, 126$ : magic  
 $Z_i$  from Segrè plot, max. stability

$$A_i = N_i + Z_i$$

plot  $A_i^{1/3}$  vs  $i$ , tag =  $N_i$



# nuclear shells

## $A^{1/3}$

2 shell lines with interesting properties:

- **cross at the first shell, He-4** ( $\delta y < 3\%$ );
- in shells 2 and 3, line #2 corresponds to values of  $A$  of  $12=6+6$  and  $28=14+14$ ; 14 recognized long ago as quasi-magic; the "magicity" of 6 is a more recent result;
- the **ratio of the cubes of the slopes of the two lines is 1.99**, very close to 2: the number of nucleons in series #2 grows from one shell to the next at a rate = 1/2 the one of series #1;
- in line #1 the "**packing fraction**" is maximal:

$$(0.916)^3 = \mathbf{0.768}$$

$$A1(n) = 2 * [\sum_{i=n,1,1} (i+1) * i] = 2 * [(n+1) * n + n * (n-1) + .. + 2 * 1]$$

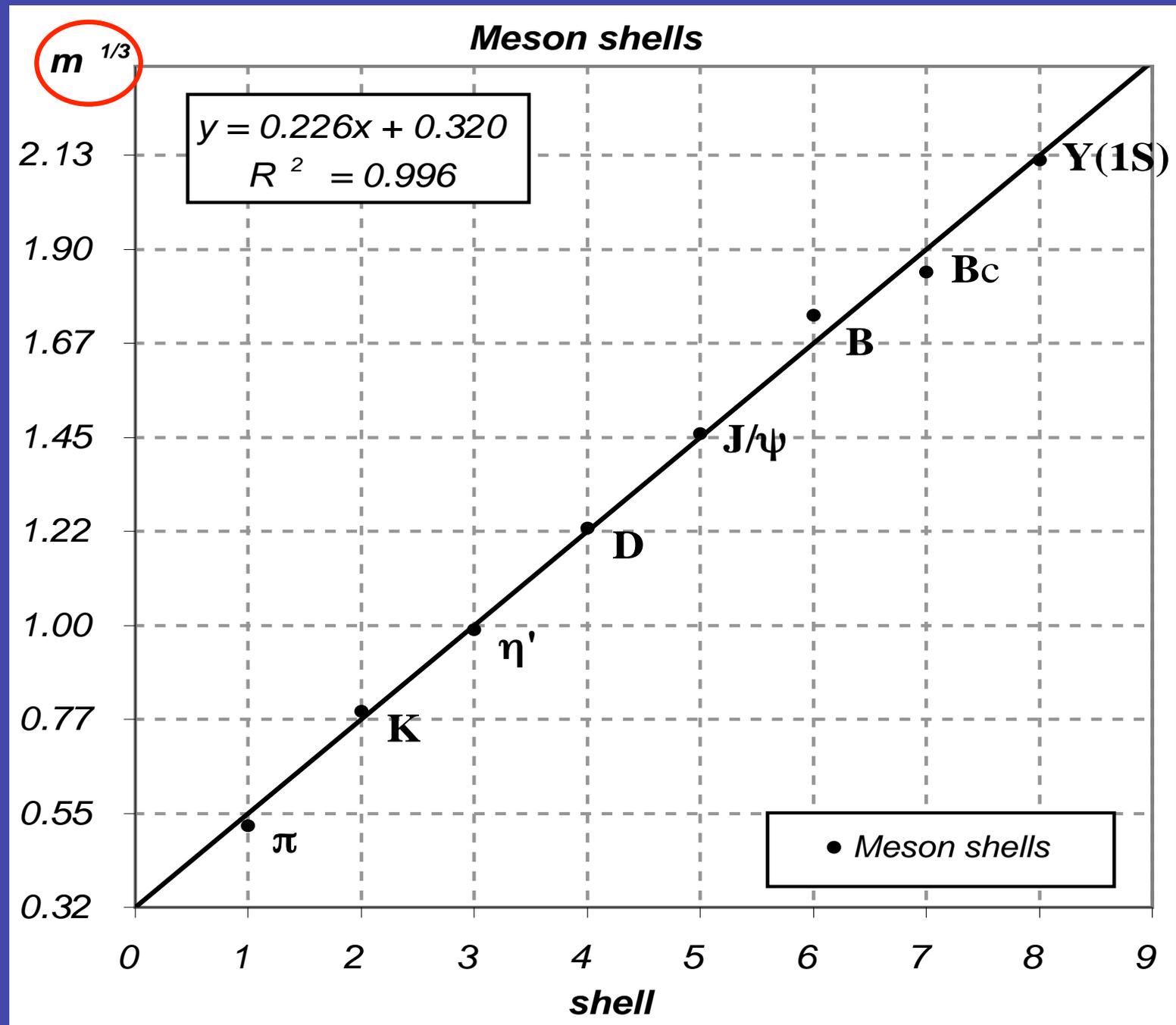
$$= 4, 16, 40, 80, \dots$$

$$A2(n) = 2 * [\sum_{i=n,1,2} (i+1) * i] = 2 * [(n+1) * n + (n-1) * (n-2) + ..]$$

$$= 4, 12, 28, 52, 88, 136, 200, 280$$



# meson shells



combine meson mass shell plot  
with mass units:

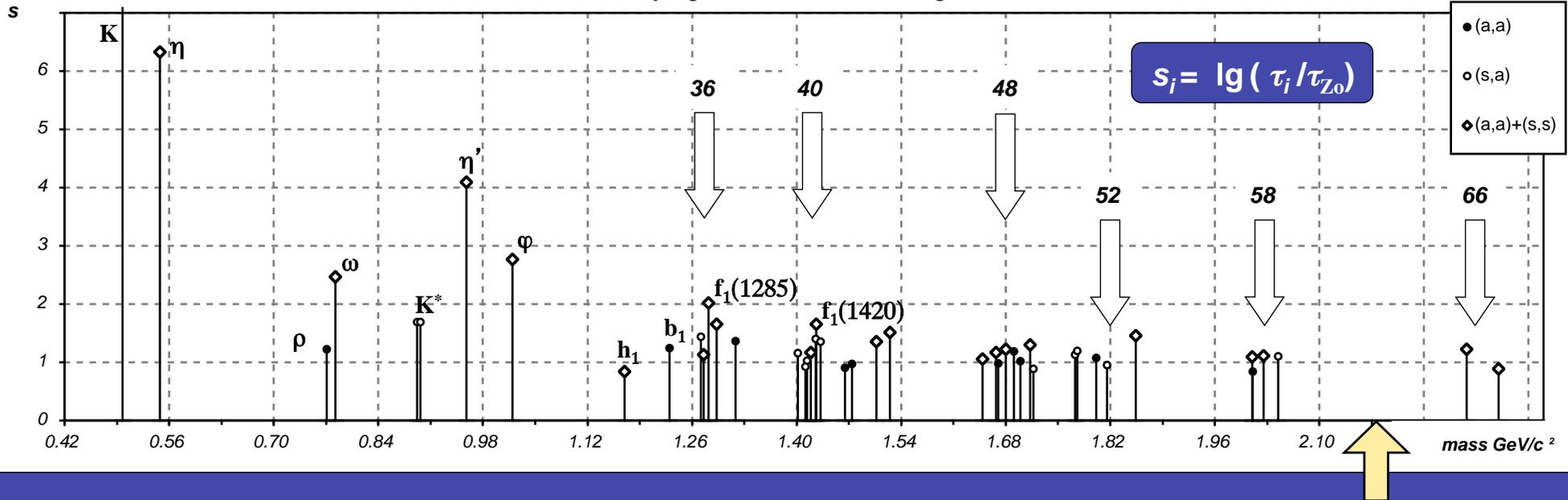
$35 \text{ MeV}/c^2 = 1 \text{ constituent}$

$M(i): (4, 14, 28, 54, 84, 152, *, 294) [i=1,8], y = 0.712 * x + 0.894, R^2 = 0.9981$

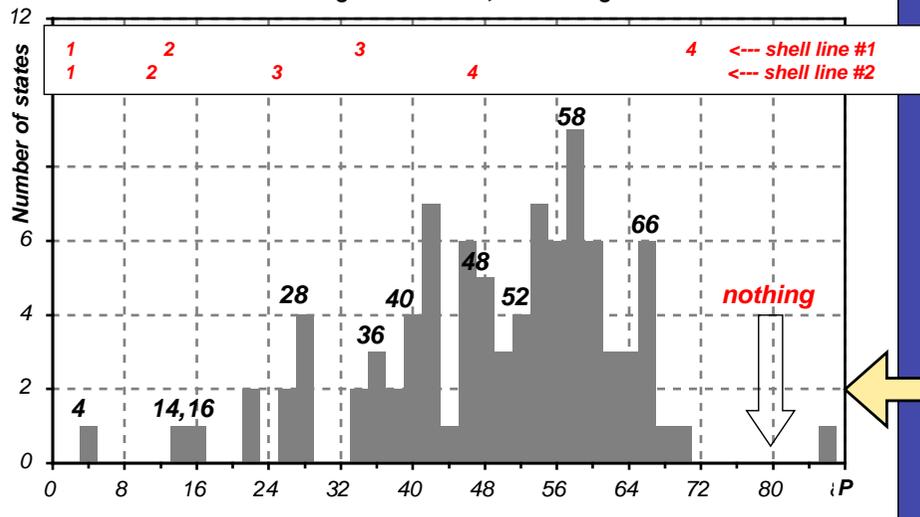
very similar to the corresponding values for the second nuclear line

$N(i): (4, 12, 28, 52, 88, 140, 208) [i=1,7], y = 0.729 * x + 0.824, R^2 = 0.9999$

### Meson stability, light unflavored, and strange mesons



### P distribution: light unflavored, and strange mesons



meson stability up to  $2 \text{ GeV}/c^2$  with mass scale in steps of  $70 \text{ MeV}/c^2$ :

- the  $\eta$  at  $P=16$ , analogous of the **doubly-magic O-16**
- three clusters around  $1260 \text{ MeV}/c^2$  ( $P=36$ ),  $1420 \text{ MeV}/c^2$  ( $P=40$ ), and  $1680 \text{ MeV}/c^2$  ( $P=48$ ).
- three further clusters with fewer states,  $\sim 1820 \text{ MeV}/c^2$  ( $P=52$ ),  $2030 \text{ MeV}/c^2$  ( $P=58$ ), and  $2310 \text{ MeV}/c^2$  ( $P=66$ ).

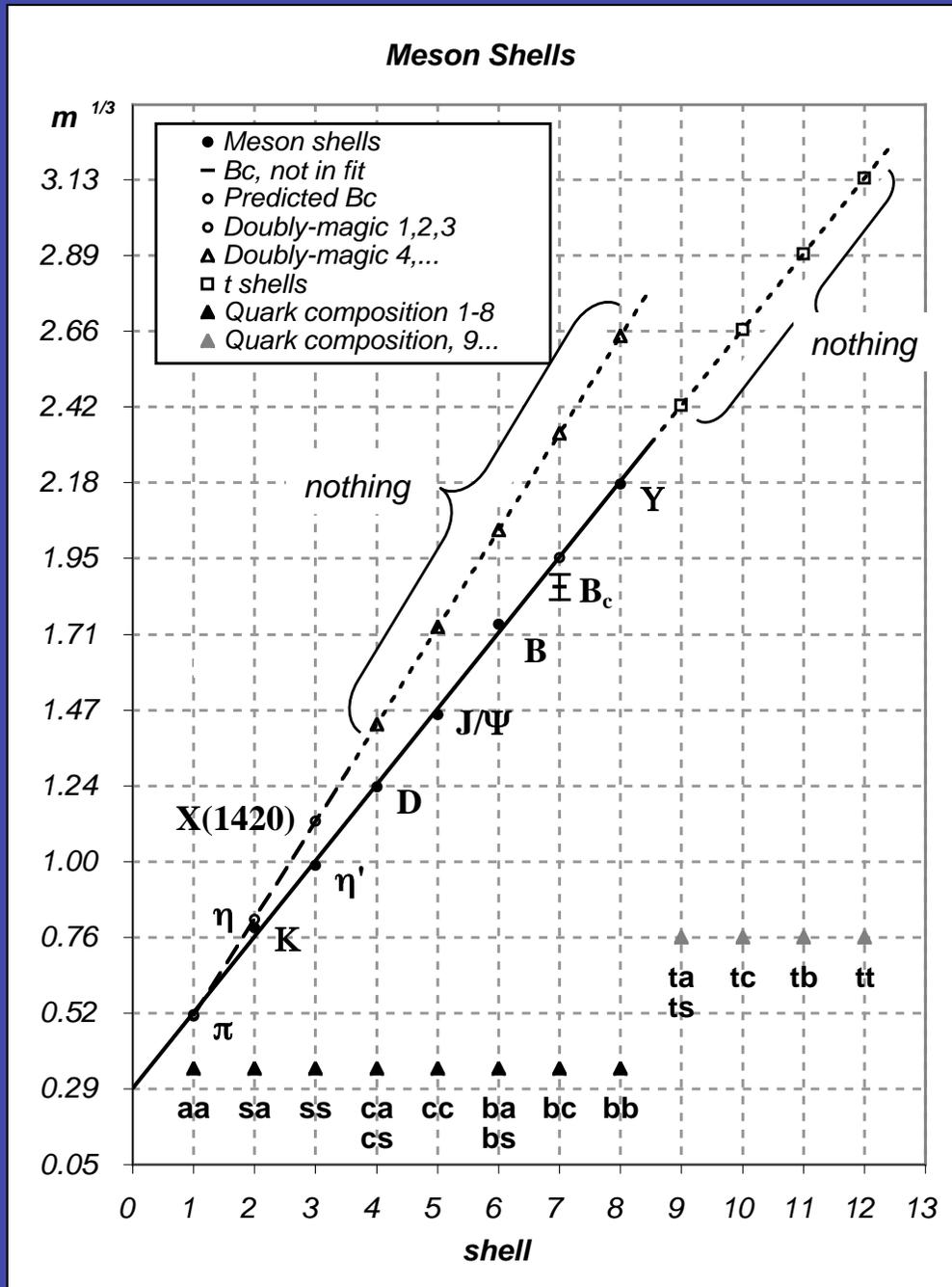
$P=40$  corresponds to shell 3 in the nuclear line #1, the **doubly-magic Ca-40**.

the  $P$  distribution for all (a,a), (s,a) and (s,s) states confirms the three clusters around **36, 40 and 48**, as well as at **52, 58 and 66**. In the shell interpretation the peaks at  $P=36, 48, 52, 58$  and  $56$  would correspond to **sub-shells** (to be developed).

$P=80$  is the **doubly-magic shell 4**  $\sim 2800 \text{ MeV}/c^2$ ; the histogram is empty from  $P=72$  to  $84$ : as in nuclei, the **doubly-magic-equivalent shell series stops at 3**.

# sub-shells

# meson shells summary

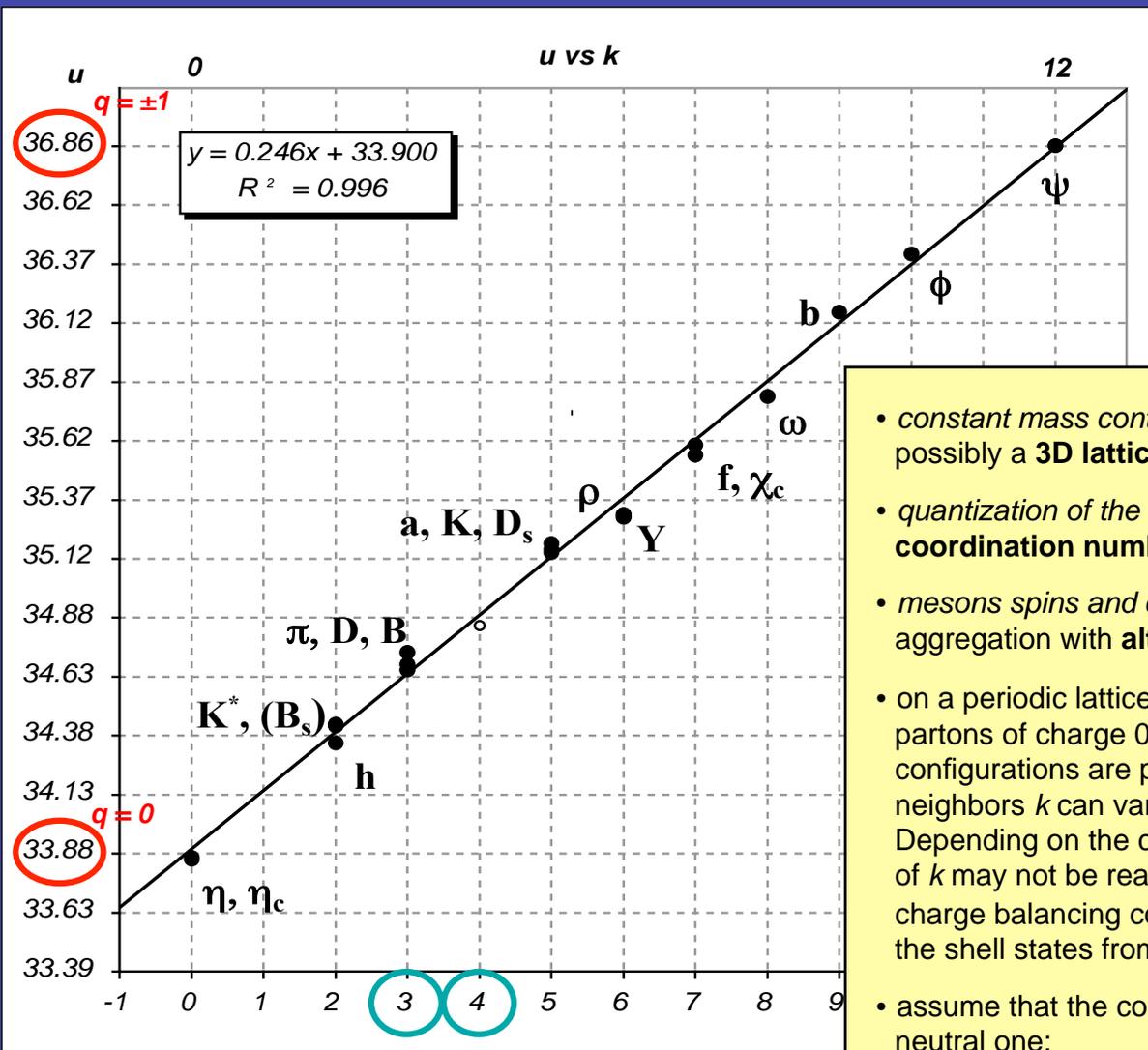


- meson shells 1 to 8 corresponds to nuclear shell line #2, and also **doubly-magic** shells can be identified:
  - 1)  $\pi$  at  $P=4 \sim \text{He-4}$
  - 2)  $\eta$  at  $P=16 \sim \text{O-16}$
  - 3) states at  $P=40 \sim \text{Ca-40}$
 but no states are known near the extrapolated mass values for the following shells in that series,  $P=80, \dots$ ;
- on the main meson shell line, the **quark composition progression** from shell 1 to 8 is:
 

**aa, sa, ss, ca+cs, cc, ba+bs, bc, bb ; (a = u or d)**

  - intriguing role of the s quark,
  - explanation of **the mysterious values of “quark masses”** (for whatever it is worth);
- **t quark:** expect 4 more shells at specific mass values in the range 14 - 31  $\text{GeV}/c^2$ , none observed;
  - is shell **8** the **structural limit** for this kind of bound states, like 6 for atoms and 7 or 8 for nuclei?
  - what are the **top events**?

$$m(t) = m(W) + m(Z^0)$$

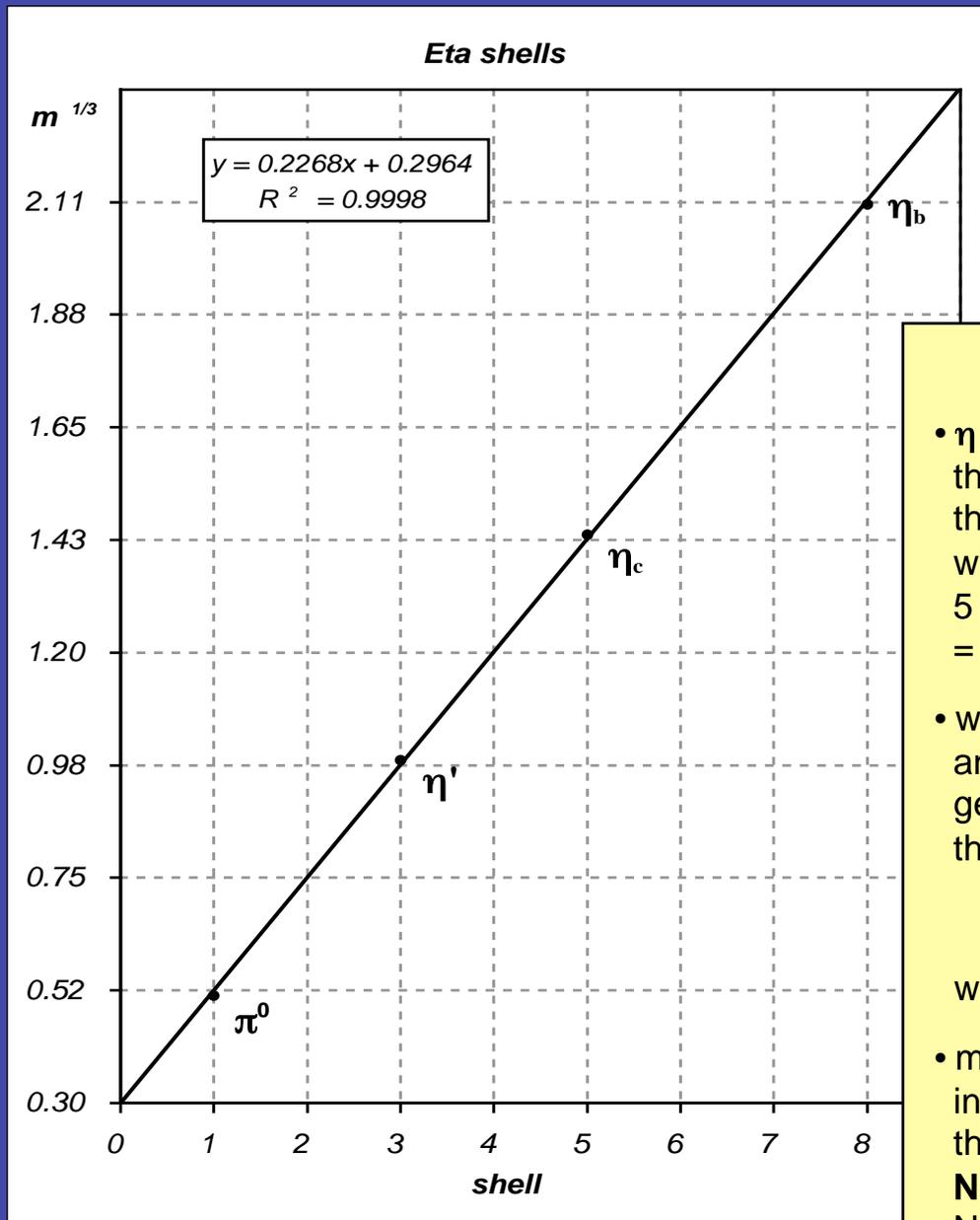


- solid-phase
- coordnum = 12: fcc
- charges

- constant mass contribution for each parton: suggests **solid-phase** aggregates, possibly a **3D lattice** organization;
- quantization of the mass unit on a grid of **13=12+1** values: may be related to the **coordination number** of the lattice;
- mesons spins and charges equal or close to 0, with a large number of partons: aggregation with **alternating up/down spins and +/- charges**.
- on a periodic lattice with **coordination number = 12** (such as the **fcc**), with spin-1/2 partons of charge 0, -1 and +1, arranged as a partially charged "ionic" lattice, several configurations are possible. For a given node of the lattice, the number of charged neighbors *k* can vary from 0 (all neutral) to 12 (all charged), **a total of 13 values**. Depending on the charge balancing constraints on these lattice variants, some values of *k* may not be realized, while other may correspond to more than one configuration; charge balancing constraints might be the reason for the deviation of the value of *P* of the shell states from series S2.
- assume that the contribution to the total mass is larger for a charged parton than for a neutral one:
  - $u(0) = 33.88 \text{ MeV}/c^2$ , neutral parton,
  - $u(12) = 36.84 \text{ MeV}/c^2$  charged parton;

this assumption agrees with the charges of the final products of the decays of the  $\mu$  (1 charged out of 3 = 4/12,  $k=4$ ) and of the  $\pi^\pm$  (1 charged out of 4 = 3/12,  $k=3$ ) as verified by the position of the corresponding points on the *u*-grid. This would not be true with the neutral parton heavier than the charged one.

# interpretation



- $\eta$  and  $\eta_c$  is at  $k=0$  on the  $u$ -grid, with **all constituents neutral**; the specific mass unit of the  $\pi^0$  is 33.74, close to  $u(0)=33.88$ , so that 4 neutral constituents can be assumed; the pion is at shell 1 with  $P=4$ , while the  $\eta'$  is at shell 3 with  $P=28$ , and the  $\eta_c$  at shell 5 with  $P=88$ , right at the nominal values of  $P$  in the series  $A2(n) = 4, 12, 28, 52, 88, \dots$

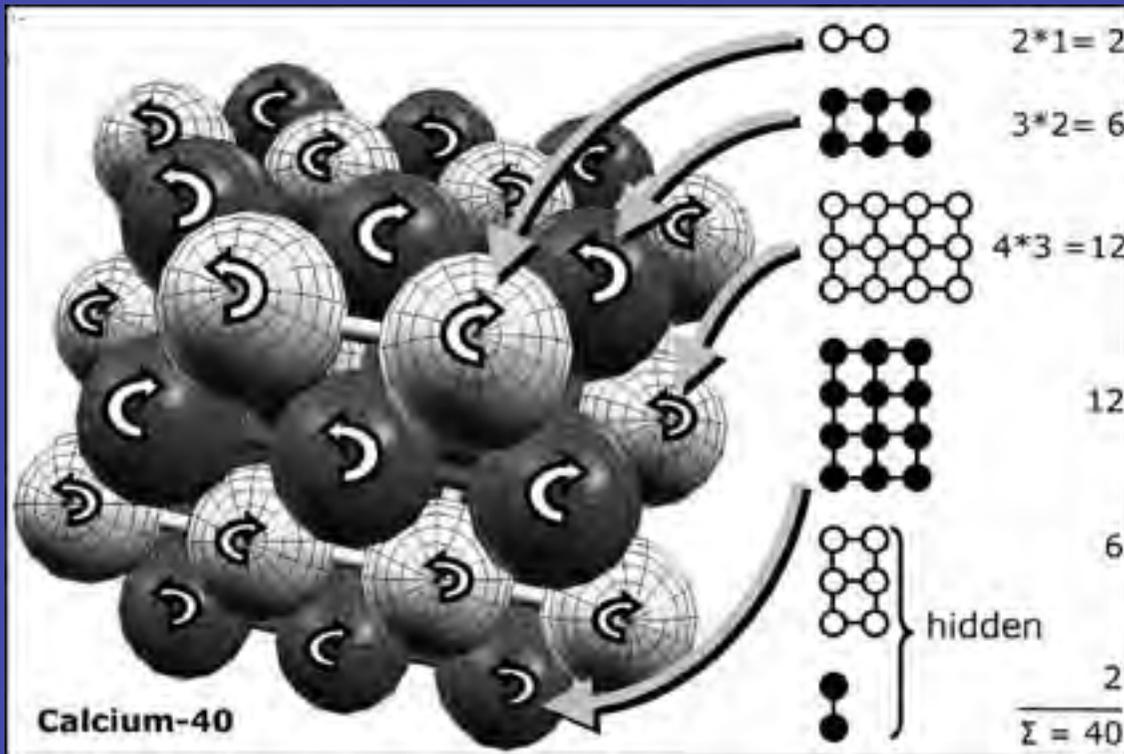
- with no charged constituents, the  $\eta$  and  $\eta_c$  do not need to obey any **charge balancing constraints** and can sit right at the geometrical shell closure; this should also apply to the  $\eta_b$ , therefore it is expected that the mass shell line with:

$$\pi^0, \eta', \eta_c, \eta_b \text{ in shells } 1, 3, 5, 8$$

would show a **sharper alignment**, as verified by the chart;

- mesons are similar to nuclei and at the same time show indications of a solid-phase fcc structure, and this may be more than a coincidence: **fcc nuclei** are not new, see the work of **Norman D. Cook**, and his recent book: Models of the Atomic Nucleus (Springer).

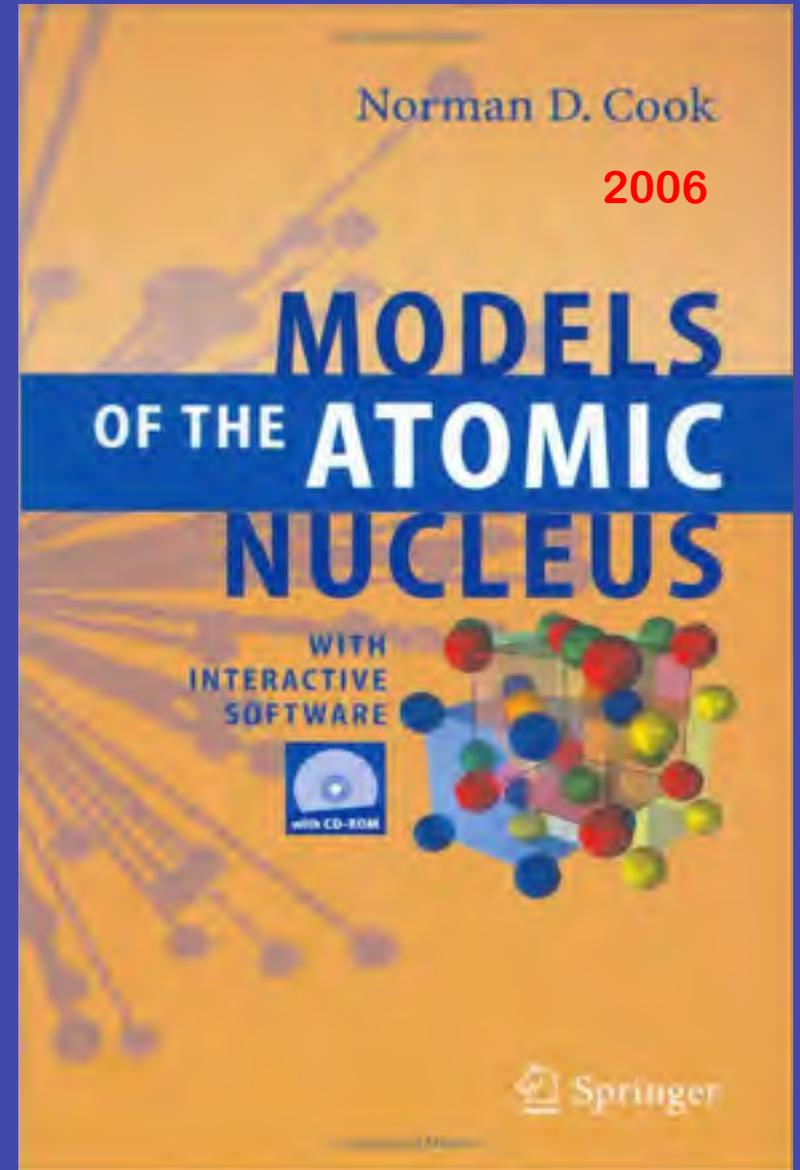
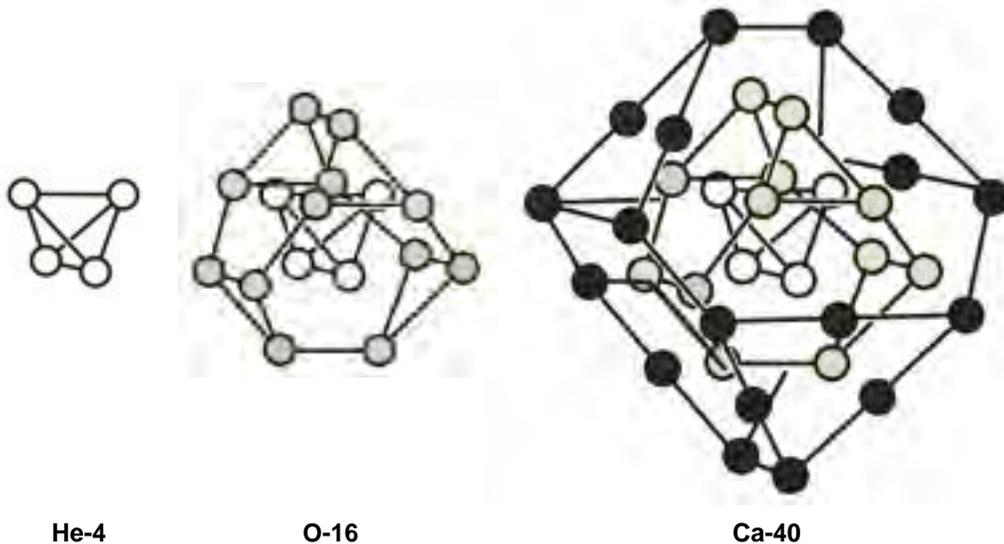
**$\eta$  shells: sharper**



$$A1(n) = 2 * [\sum(i+1)*i, i=n,1,1] = 2 * [(n+1)*n + n*(n-1) + \dots + 2*1]$$

$$A2(n) = 2 * [\sum(i+1)*i, i=n,1,2] = 2 * [(n+1)*n + (n-1)*(n-2) + \dots]$$

[ tetrahedrally-truncated tetrahedrons ]



Looking for neutral and charged partons and antipartons with spin  $1/2$  and mass less than  $30 \text{ MeV}/c^2$ , and with **more than one type of neutrals**, among the known particles there is only one possible choice:

**the stable leptons -->**

**constituents:**

**stable leptons?**

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## STABLE PARTICLES AS BUILDING BLOCKS OF MATTER

1980

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Boulder, Colorado 80309

Only absolutely stable indestructible particles can be truly elementary. A simple theory of matter based on the three constituents, proton, electron and neutrino (and their antiparticles), bound together by the ordinary magnetic forces is presented, which allows us to give an intuitive picture of all processes of high-energy physics, including strong and weak interactions, and make quantitative predictions.

### I. INTRODUCTION

**SU(3) from permutations**

At present, the picture of elementary particle physics mostly used in high-energy phenomenology is becoming admittedly very complicated. Besides leptons (which we see), one introduces families of "quarks", each with different colours, then the so-called "gluons", which are the gauge vector mesons binding the quarks, then there are the so-called "Higgs particles", which give masses to some of the vector mesons (all of which are not seen in the laboratory). One is already beginning to talk about a second generation of more fundamental and simpler objects for these quarks and gluons etc., even though these first generations of "basic" objects have not been seen. This type of framework seems to create more problems than it solves <sup>1)</sup>.

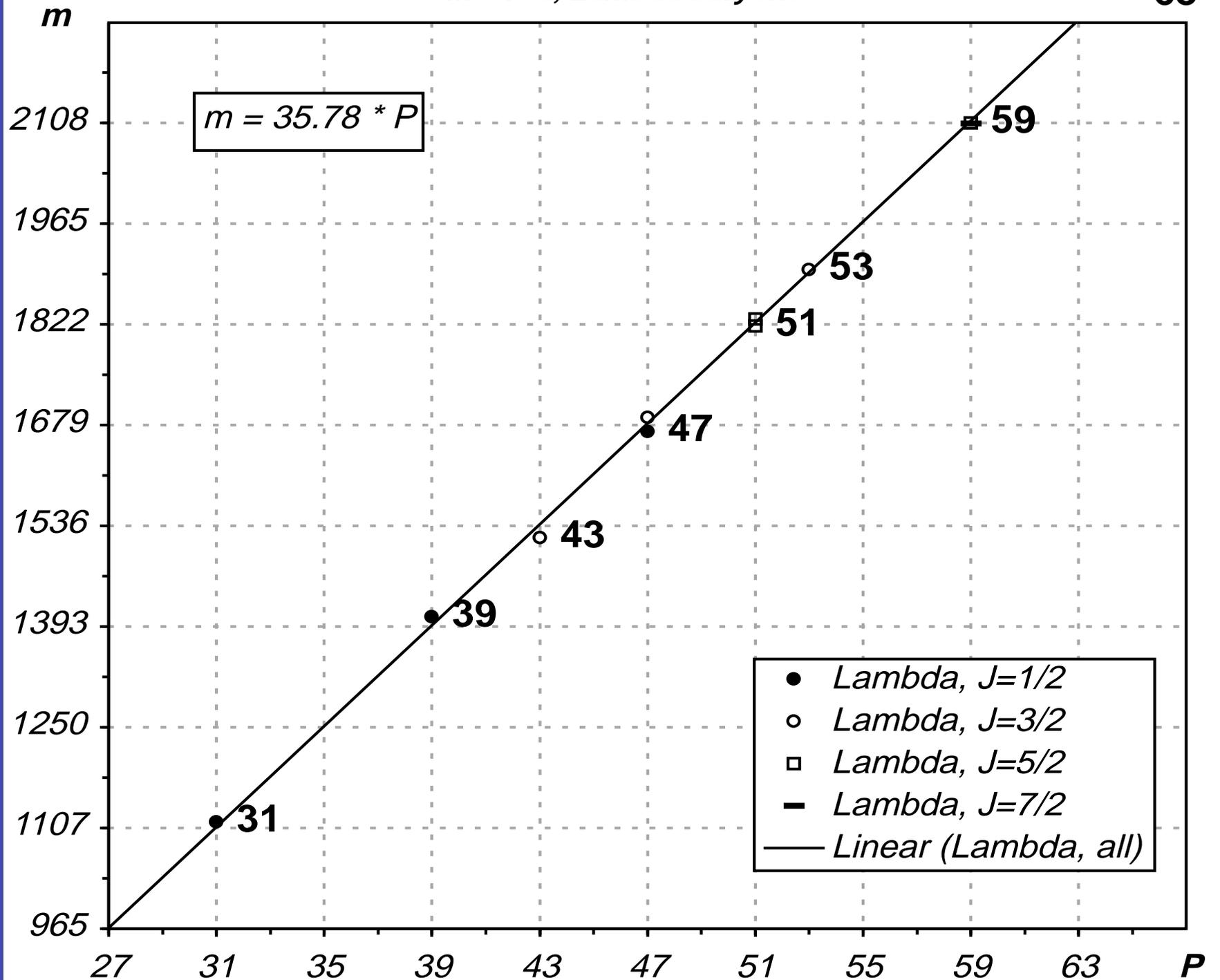
**the baryon mass system**

same analysis,  $P$  is odd



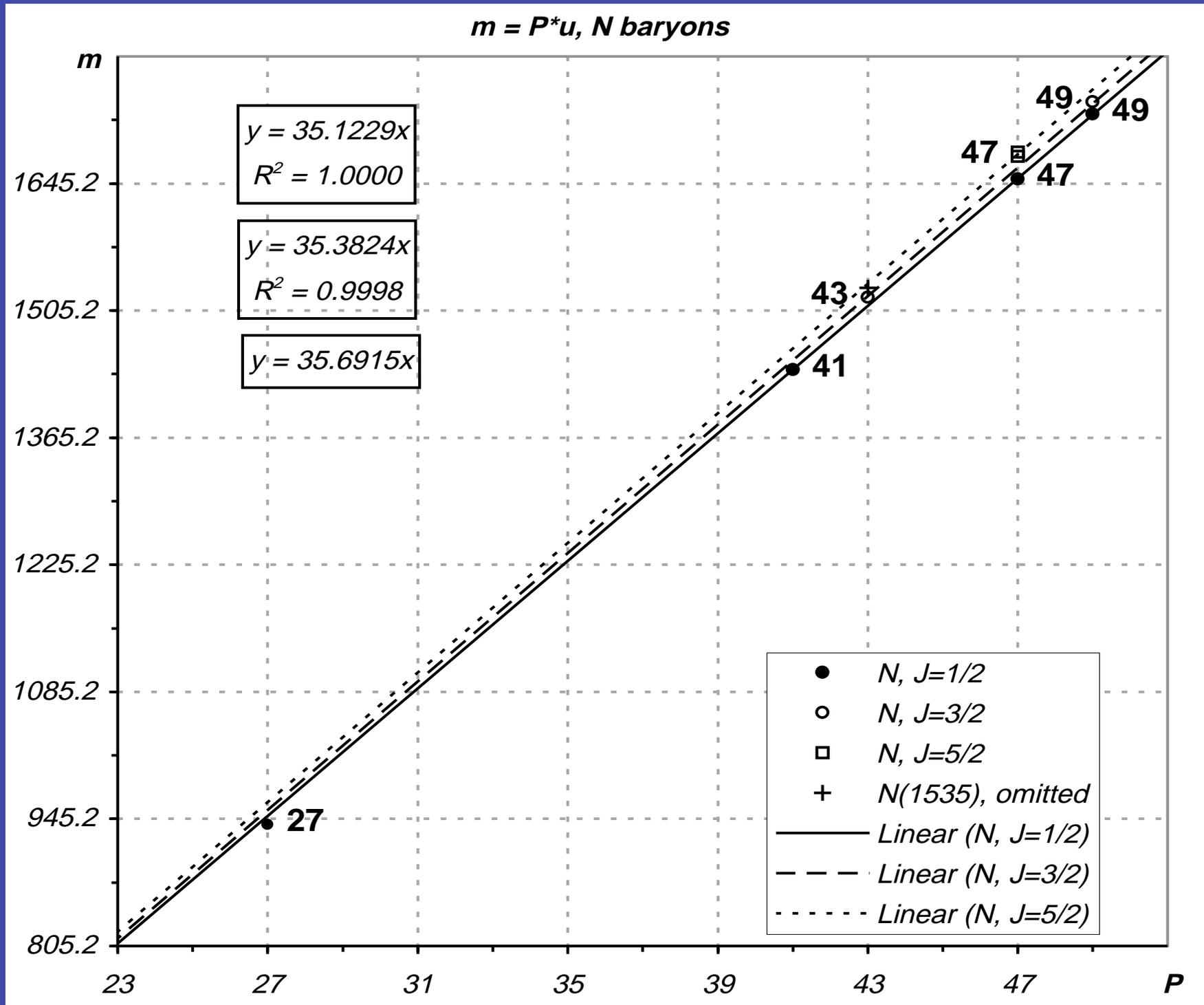
$m = P \cdot u$ , Lambda baryons

65

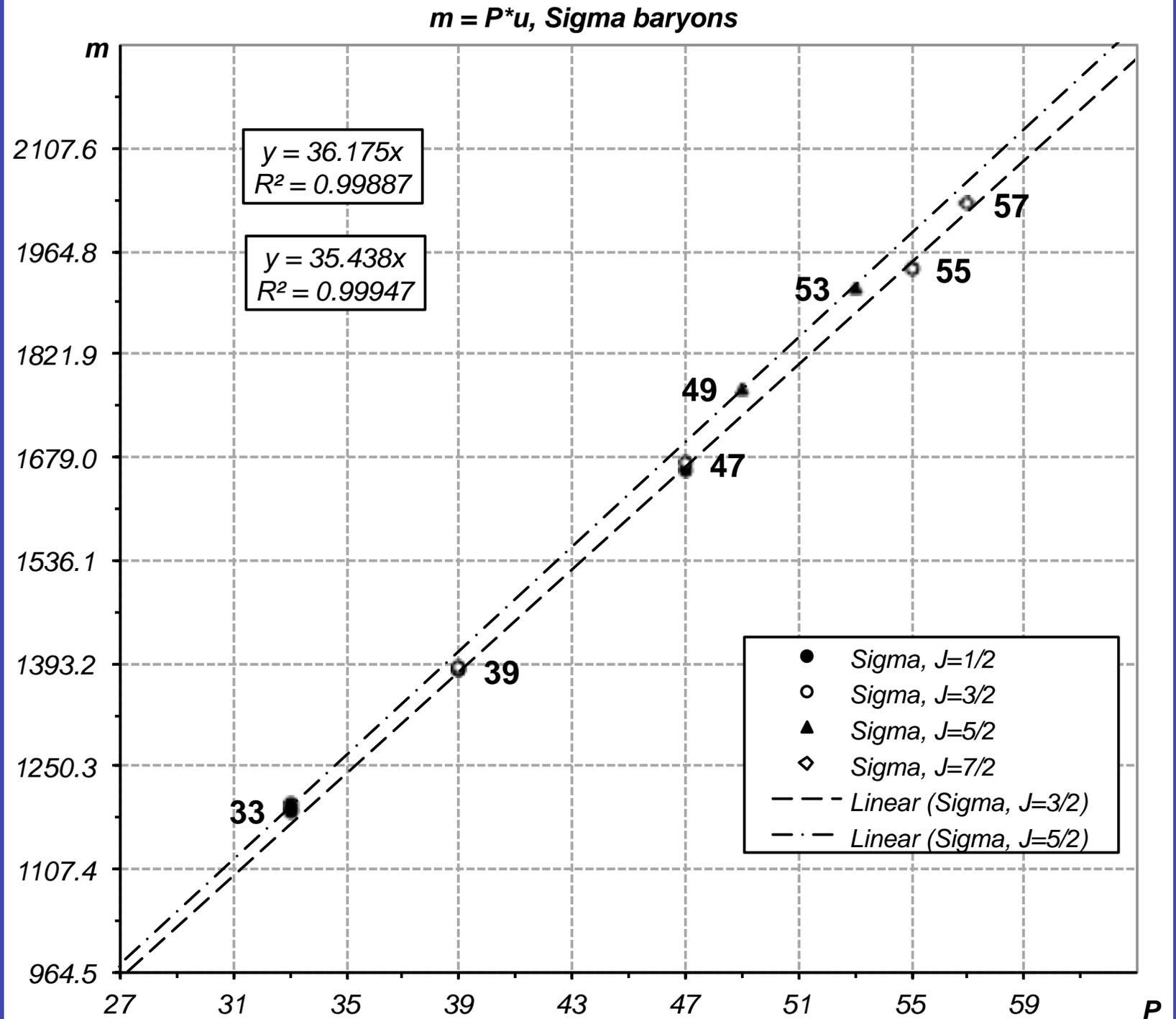


# N

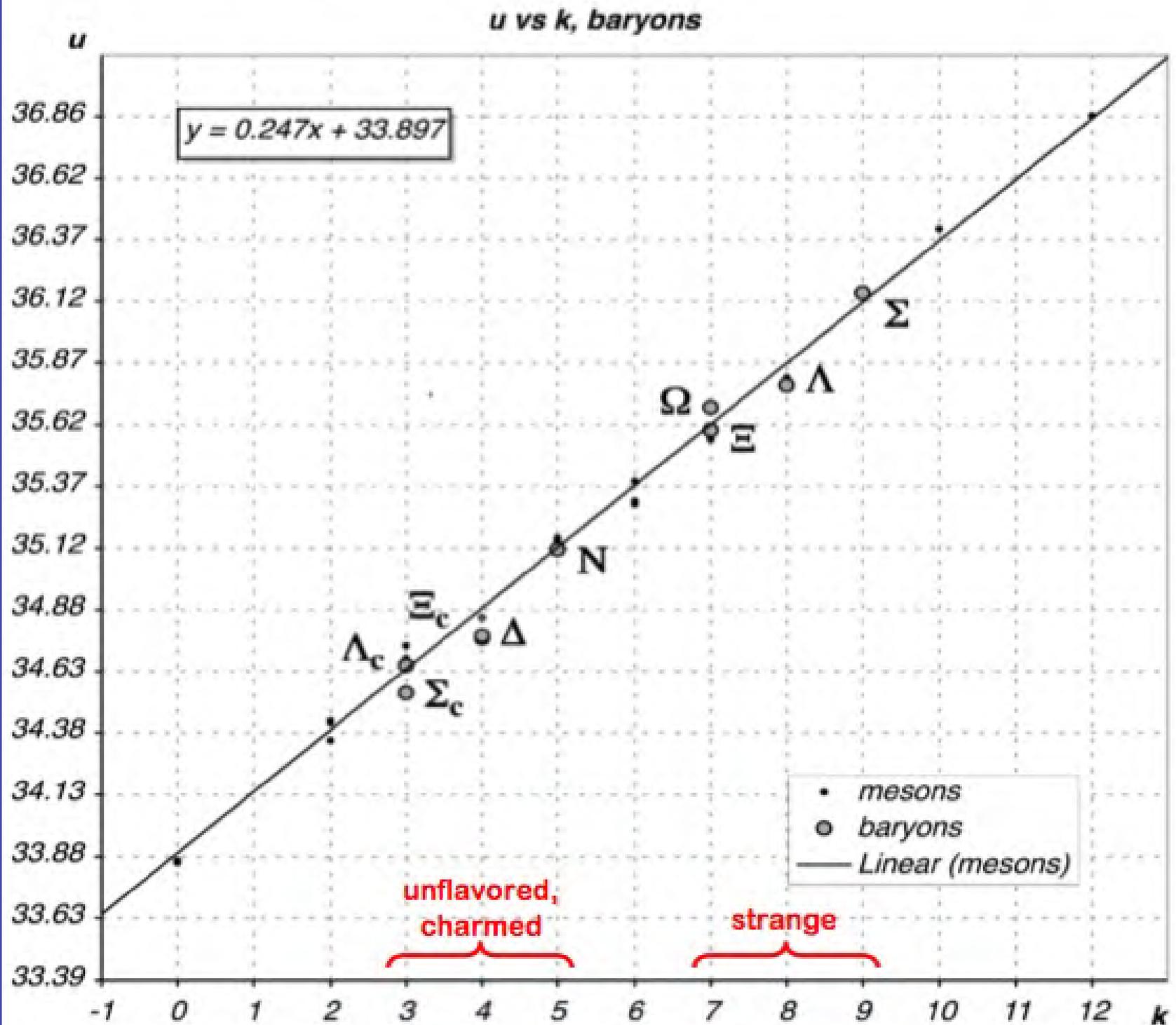
## du/dJ



# $\Sigma$ du/dJ flip-flop



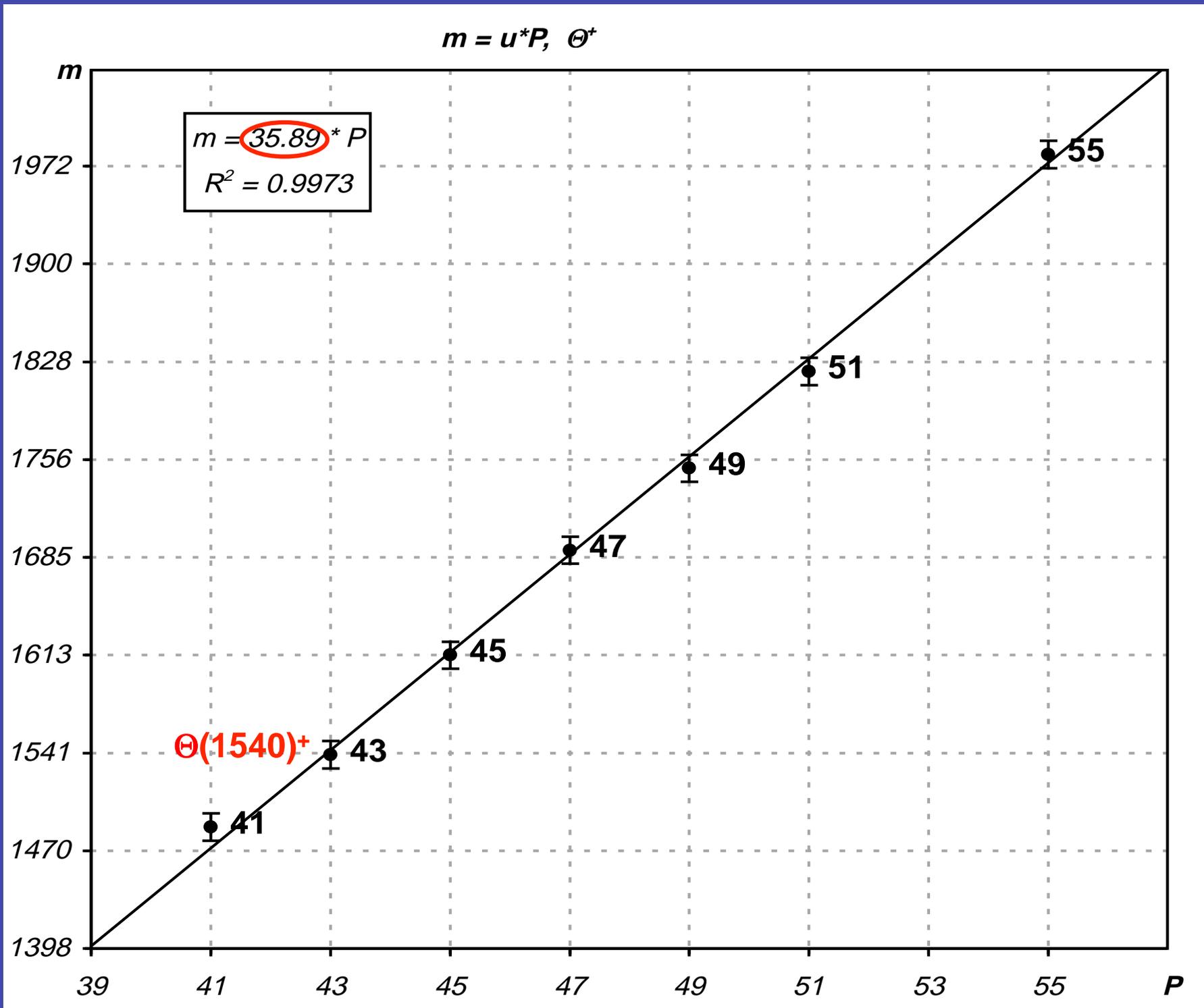
# u vs k





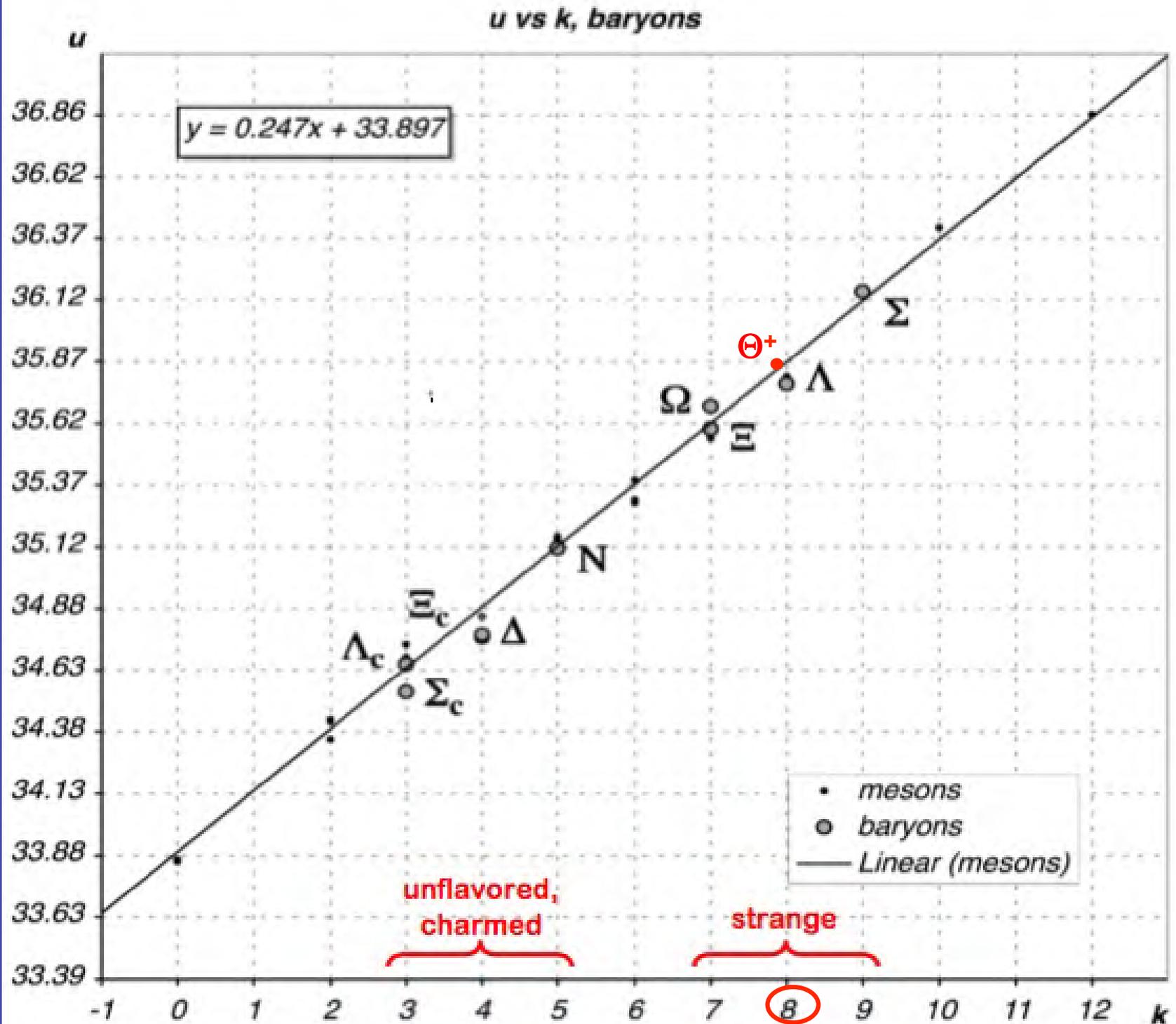
7 states

P. Aslanyan



# u vs k

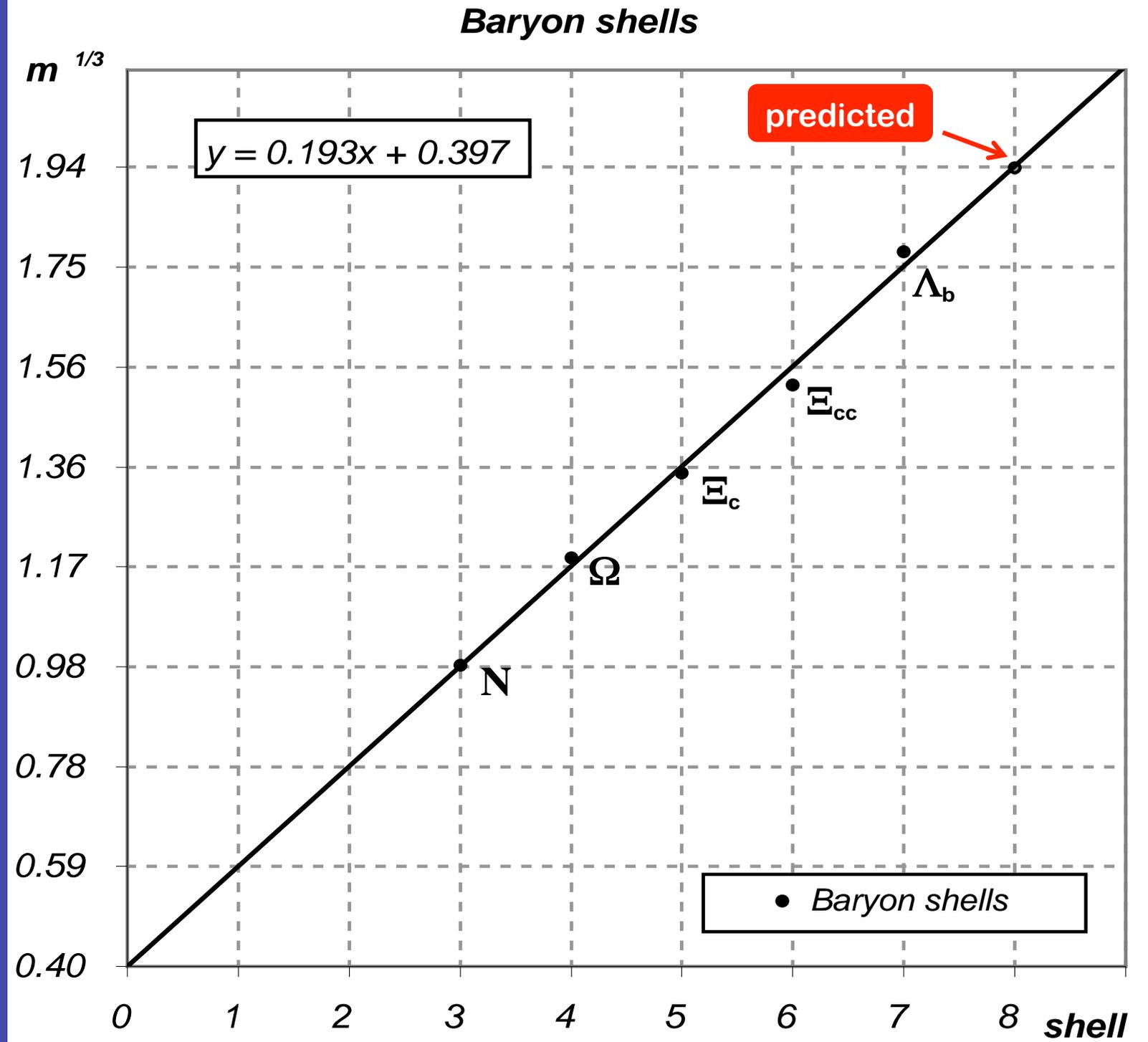
$\Theta^+$



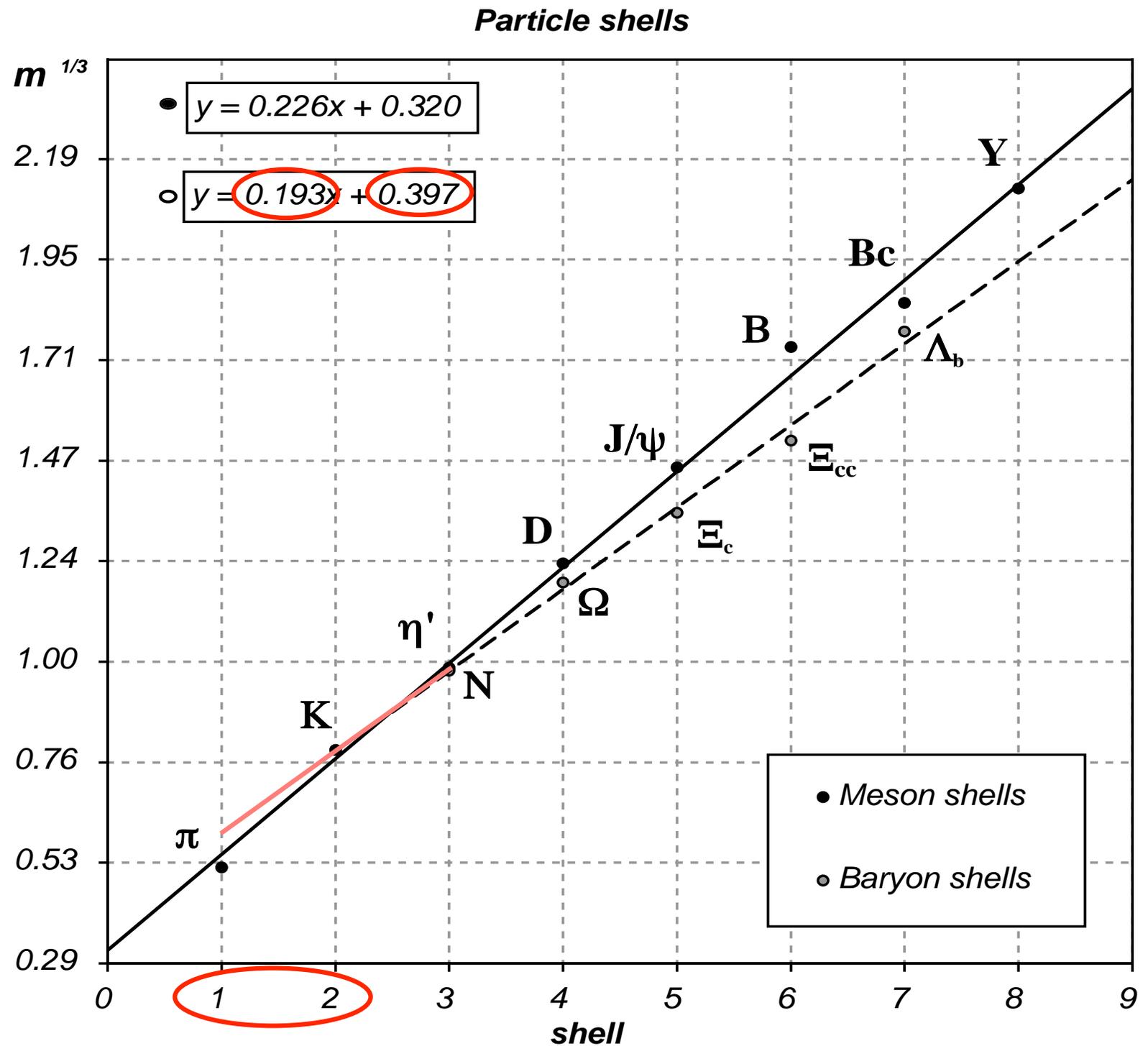
**baryon shells**



# baryon shells



# baryon vs meson shells



## baryon shells organization, clues:

- shells 1 and 2 are not cohesive
- packing density  $\cong 1/3$  of the full FCC
- 6 nodes at shell 1

diamond lattice? maybe...

**interaction**

Q uantum

sure

~~C hromo~~

no need, lattice

~~D ynamics~~

none, in 1<sup>st</sup> approx

Barut 1980

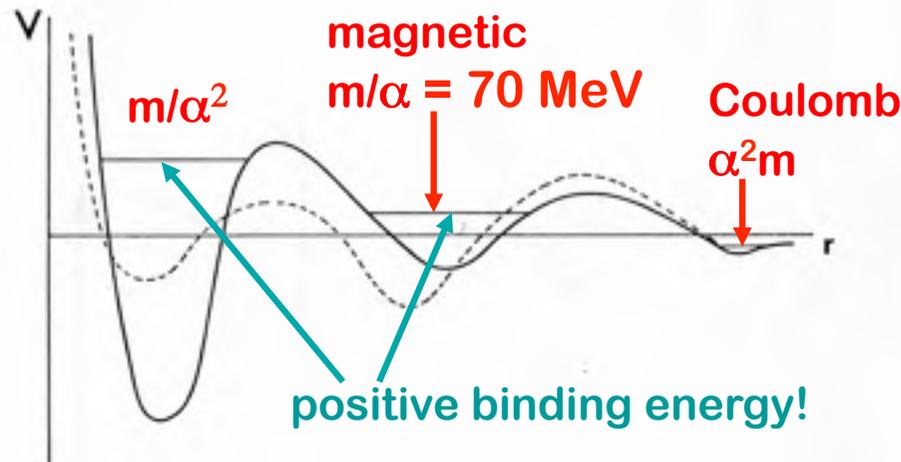


FIGURE 1. Schematic form of the effective radial magnetic potential  $V$  as a function of the radial distance  $r$  for two different fixed values of energy and angular momentum.

Q uantum  
M agneto  
S tatic

# implications

- quark-lepton relationship elucidated
- "quark masses" rationalized
- color is not needed
- baryon number may relate to a different lattice
- antimatter asymmetry shifts from the universe to the atom
- 13 out of the >26 SM parameters are gone
- electro-strong unification
- $\alpha_s$  computed in bound state =  $0.101 \pm 0.0014$

## problems

- top, but  $m(t) \cong m(Z) + m(W)$
- ...

LE CINÉMA FRANÇAIS

JEAN GABIN  
IDIA PARLO  
PIERRE BRESSAN  
ERIC STROHEMI

dans  
**LA GRANDE ILLUSION**

Un film de  
**JEAN RENOIR**

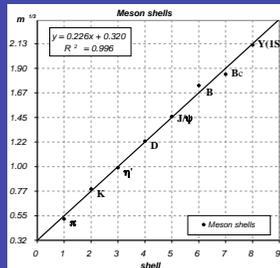
avec  
GARETTE MODOT PECLLET  
et  
**DALIO**

**GRAND PRIX DU JURY INTERNATIONAL DE VENISE**

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# Thank you for your attention !



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